

Small angle scattering techniques (neutrons and X-rays) applied to self-assembled systems, polymer networks, and nanocomposites (under deformation)



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UNIVERSITÉ
DE MONTPELLIER

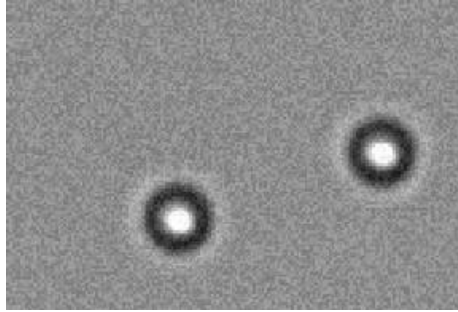


SoftComp
SOFT MATTER COMPOSITES

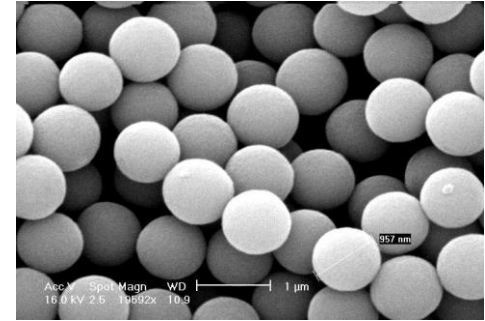
DoDyNet Winter School

January 2019

Building blocks of soft matter

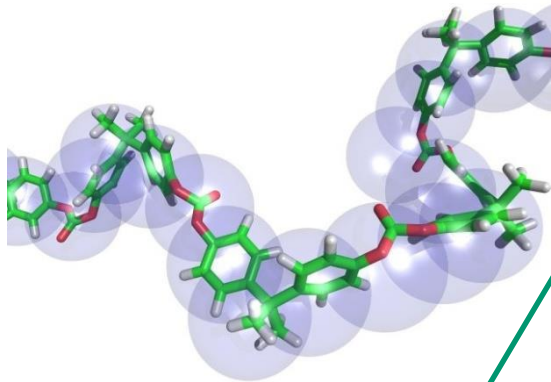


colloids

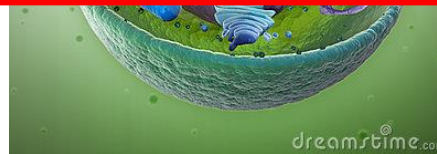


cells

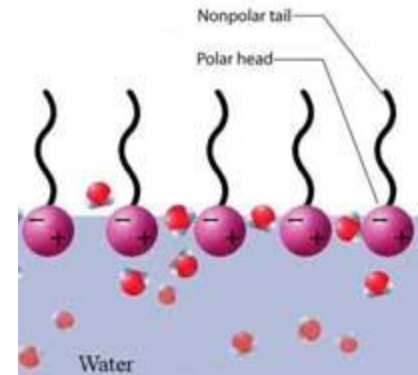
**Order on the mesoscale
= can be studied by small-angle scattering (SAS)**



polymers



liquid crystals

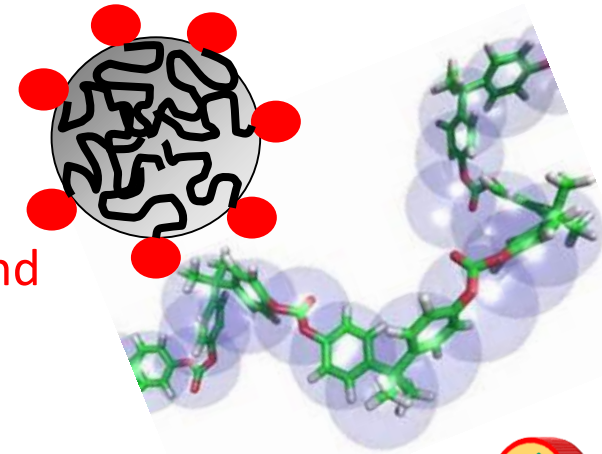


self-assembled systems

Outline

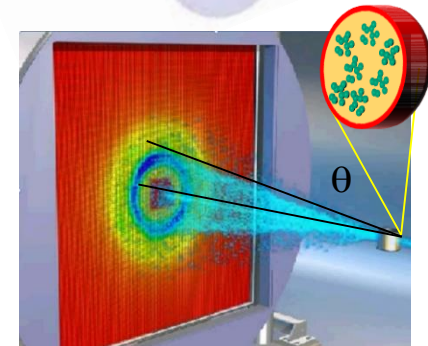
1) Soft matter as microstructured systems

- Surfactant self-assembly
- Polymer systems: molecules, networks, particles and nanocomposites



2) Structural analysis by small-angle scattering

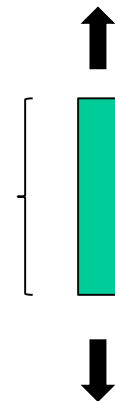
- Principles: contrast, scattering process
- Shape analysis, a 'math-free' Fourier transform
- Applications: micelles, bilayers, polymers, surfaces, aggregates
- Interactions and pair correlation



3) Scattering under deformation

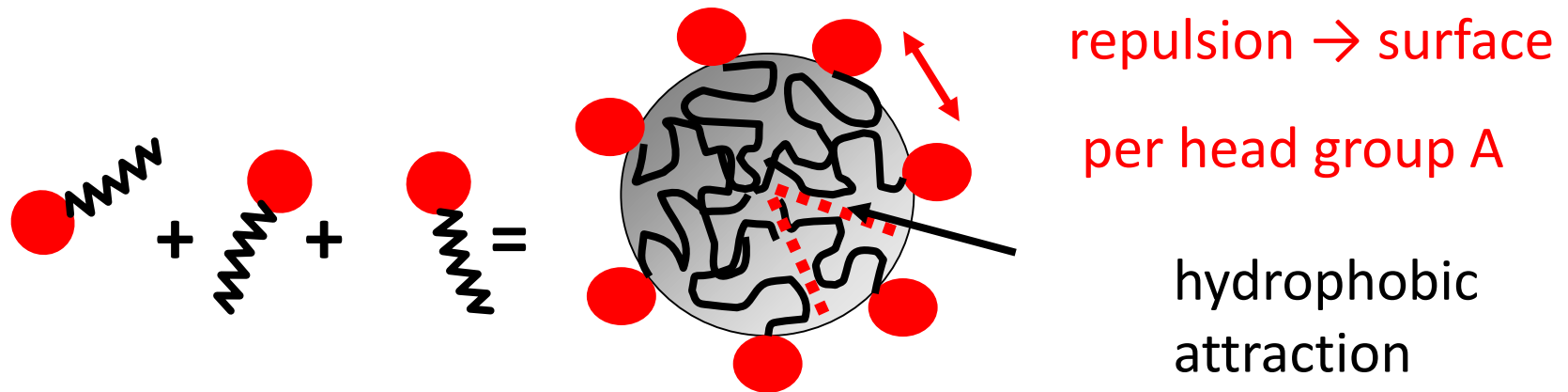
- Experiments and geometries
- Affine deformation and networks

$$L = \lambda L_0$$



Self-assembly

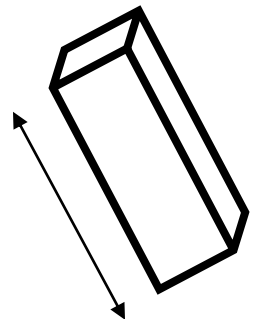
Above the critical micellar concentration (cmc), surfactant molecules self-assemble:



Spontaneous curvature of monolayer: 'geometric' packing constraints

Packing parameter $p = v/l_c A$

$R \leq l_c$ (chain extension)



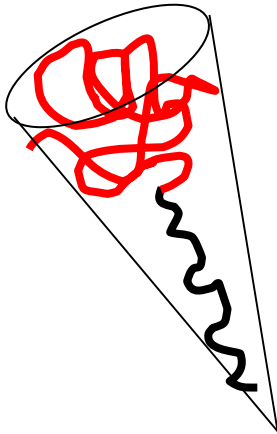
Israelachvili, Mitchell, Ninham, *J Chem Soc Farad Trans* **1976**, 1 72,1525

Israelachvili, 'Intermolecular and Surface Forces', Academic Press **1995**

Schematic phase diagram of non ionic surfactants

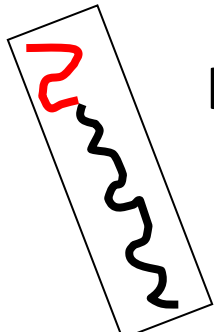
(T=const.)

Surfactant: POE



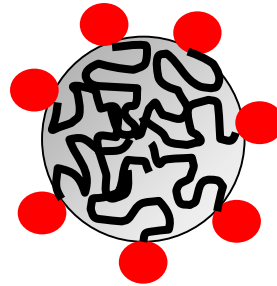
$$p = 1/3$$

Cosurfactant: pentanol, hexanol,

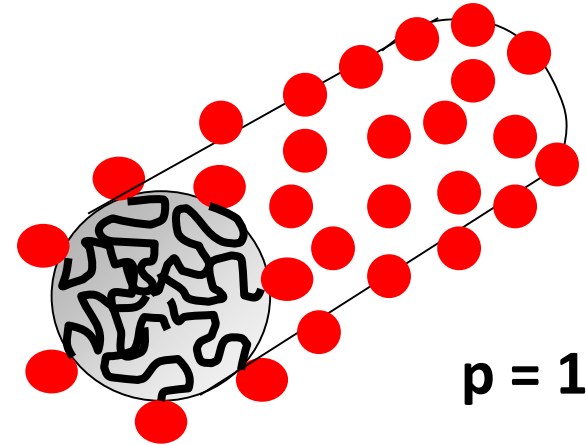


$$p = v/l_c A = 1$$

globular micelles

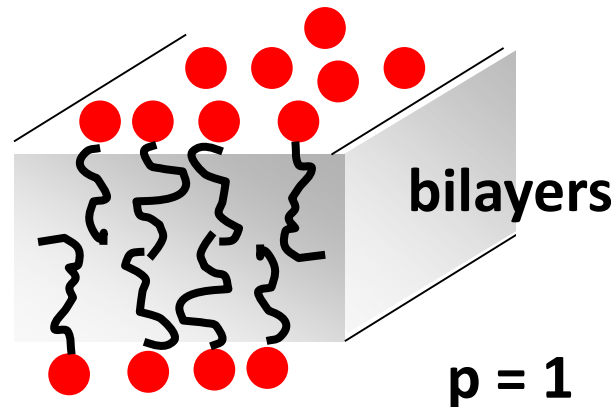


$$p = 1/3$$



$$p = 1/2$$

cylindrical micelles



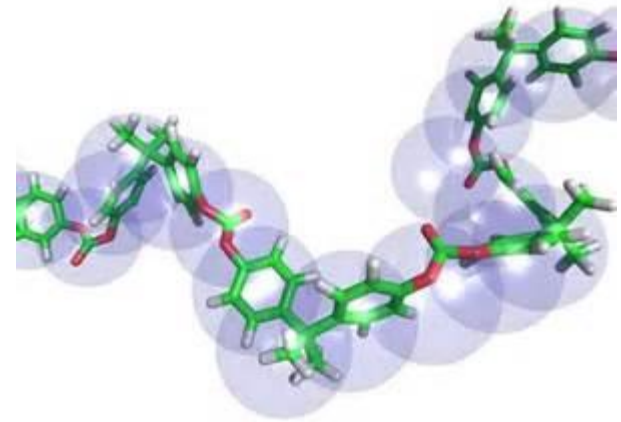
$$p = 1$$

Polymer chains

Linear polymer chain (e.g. PEO, PE, PS):



Extended length **1.5 microns**
 $\approx 10^4$ bonds ≈ 150 kg/mol



In (theta-)solvent: **$R \approx 15$ nm**

- Number of conformations: $3^{10'000} \approx 10^{5000}$
- One picosec/conformation: (much) longer than age of universe

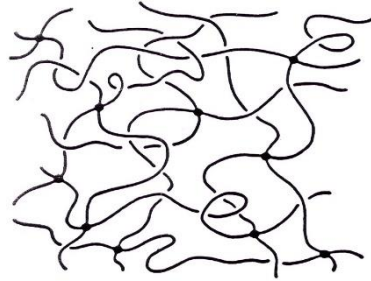
→ statistical description: **$R_g = a N^{1/2} \sim M^{1/2}$**

How can this be measured?

Polymer systems

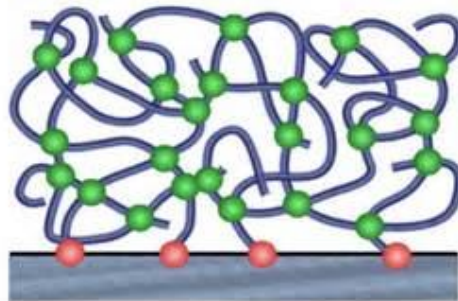
Polymer networks and gels:

with solvent; or dry
(melt or elastomer)



swelling

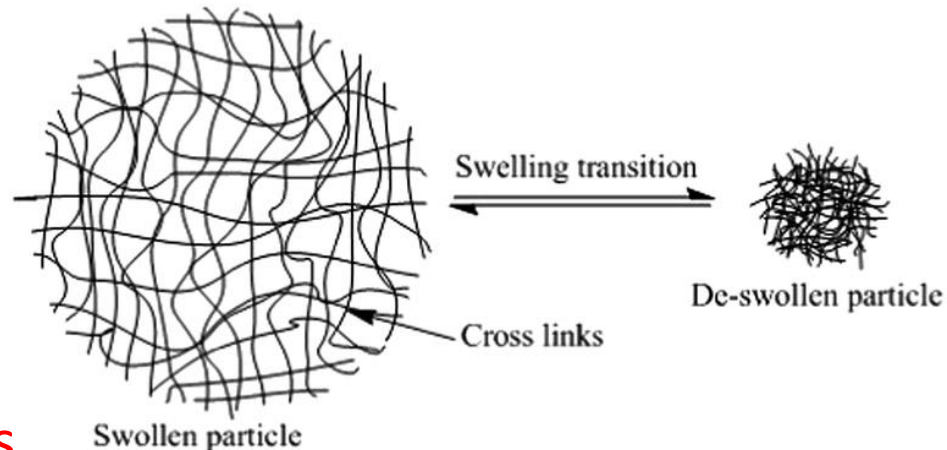
Polymer brushes:



colloidal stability;
lubrification

Polymer microgels:

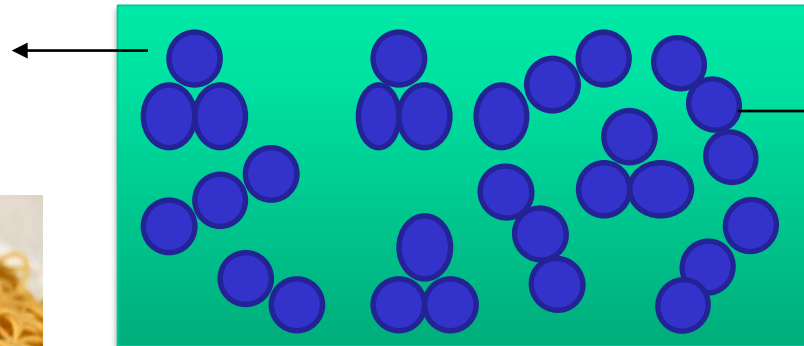
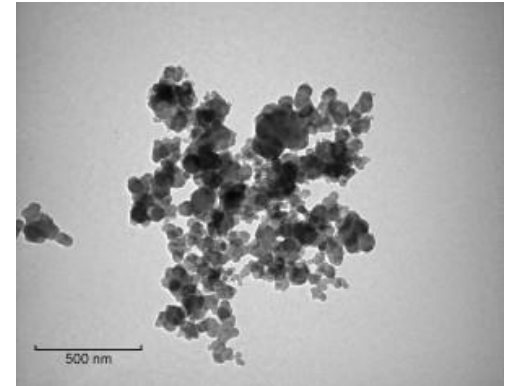
+ others: latex, polymer
adsorption,
interpenetrated networks



Polymer nanocomposites



multiphase materials
polymer + nanoparticles



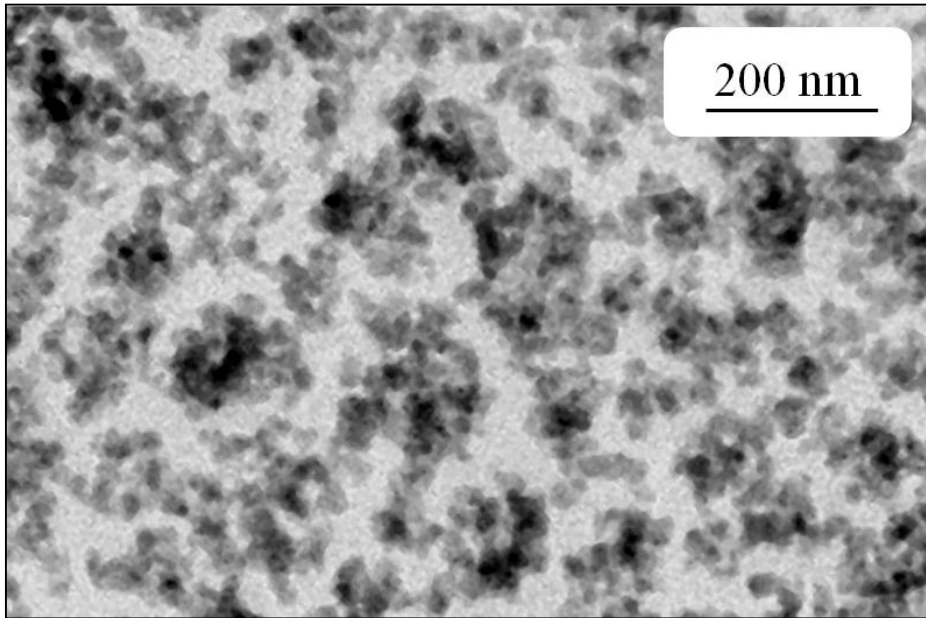
filler
(1 to 100 nm)



What is the structure of nanocomposites ?
Chain structure ? Filler structure ?
How to see one OR the other ?

How to measure structure of soft matter?

With electron microscopy:



Advantages:

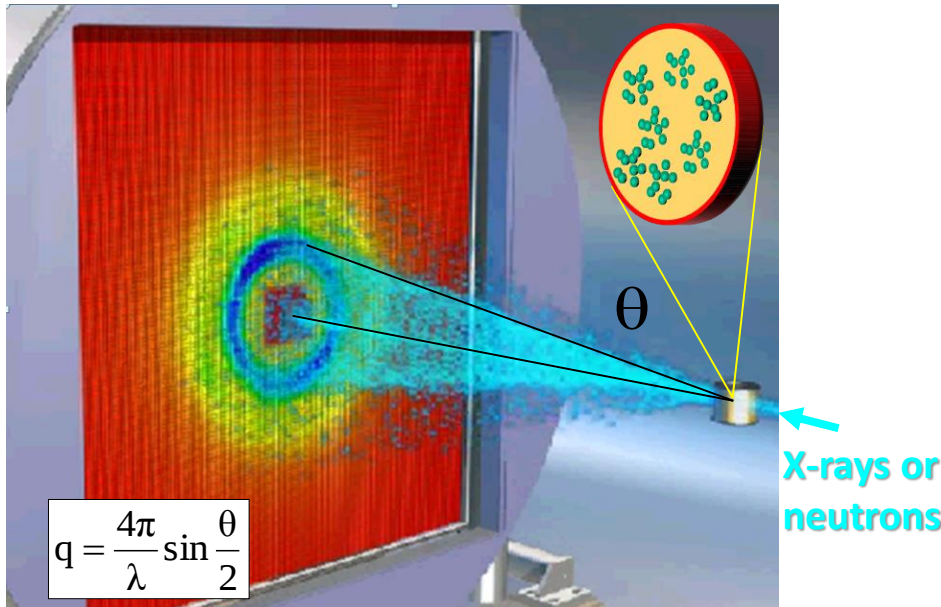
- Analysis is intuitive and simple

Problems:

- Only for filler, not chains
- 3D ?? (if not tomography)
- Statistical relevance ??

How to measure structure of soft matter?

By small-angle scattering:



Advantages:

- Statistically relevant (large sample)
- Fast and simple

Problems:

- Need contrast
- Exact **inversion** impossible: complex data analysis

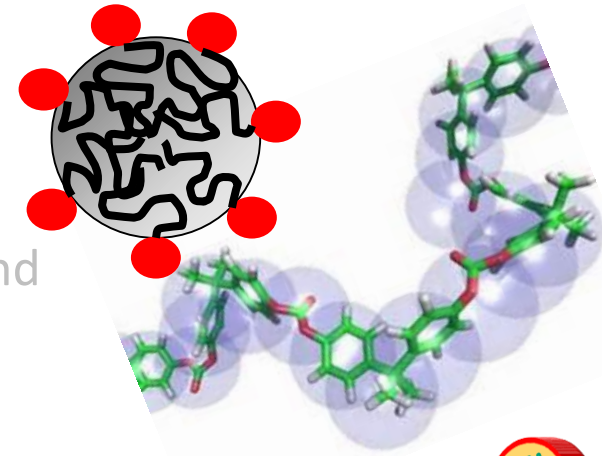
→ Combine with other information:

- A priori knowledge of system
- Different techniques, in particular imaging

Outline

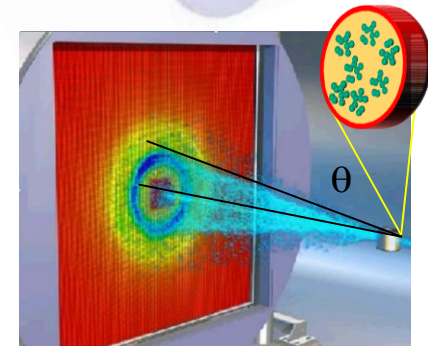
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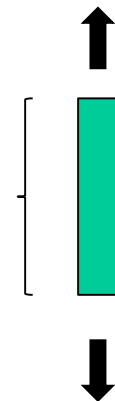
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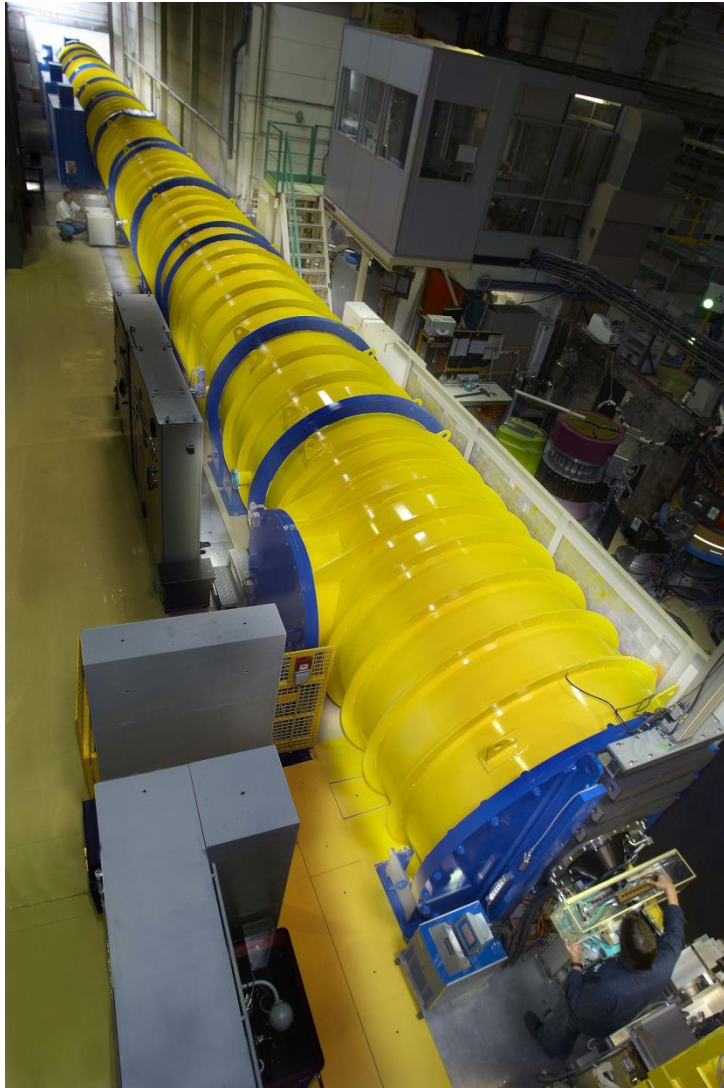
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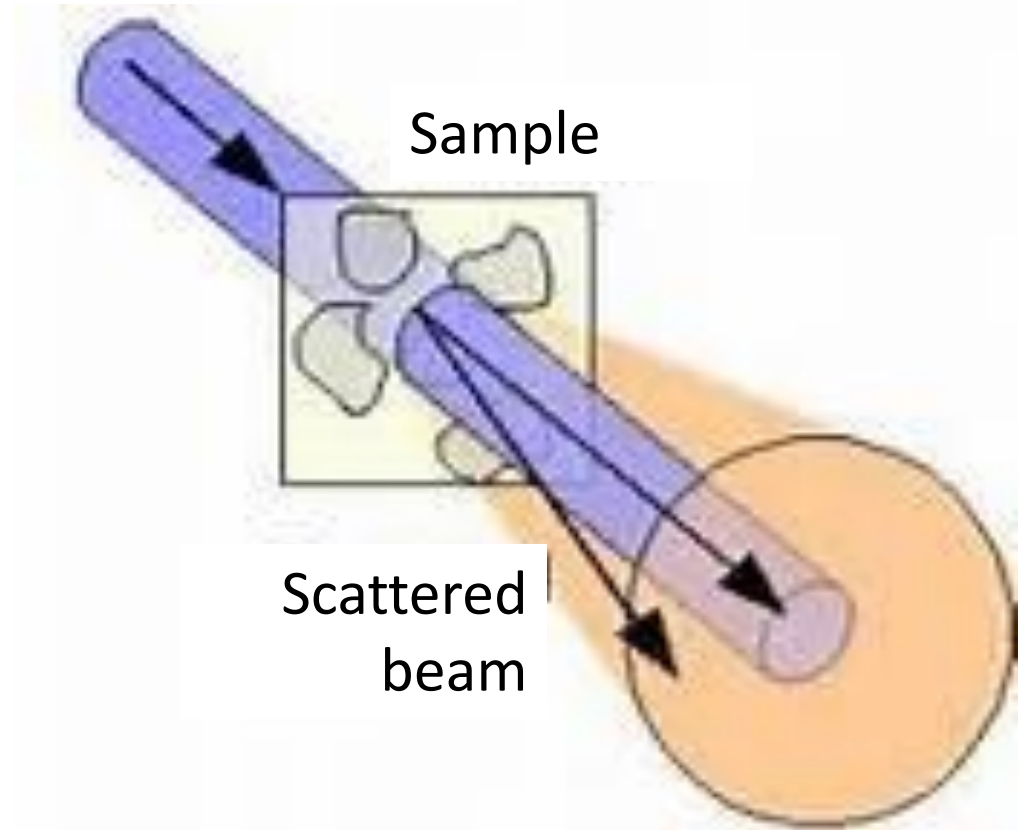


Small Angle (Neutron) Scattering: real instruments



D11, ILL Grenoble

Neutrons
or X-rays



Fourier transform !

Contrast

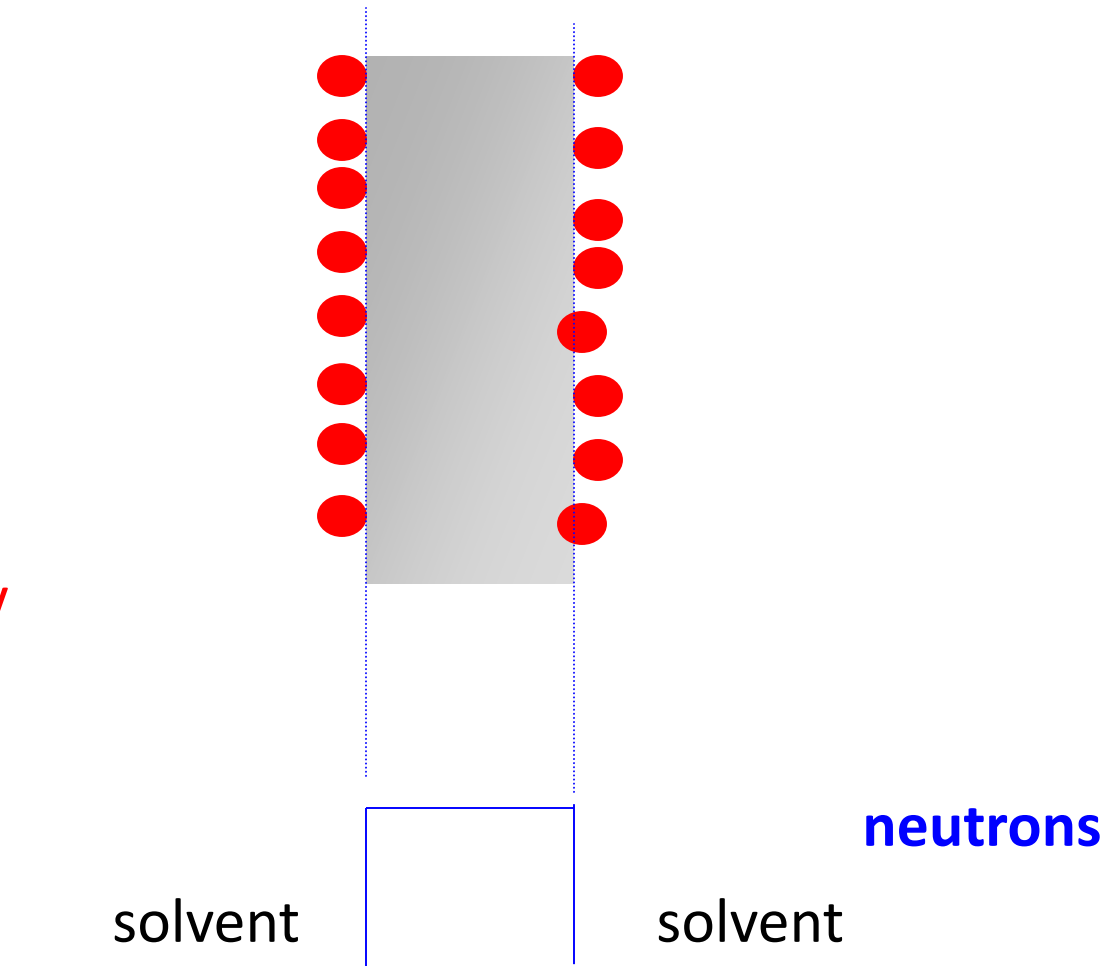
Contrast =

Difference in

scattering length

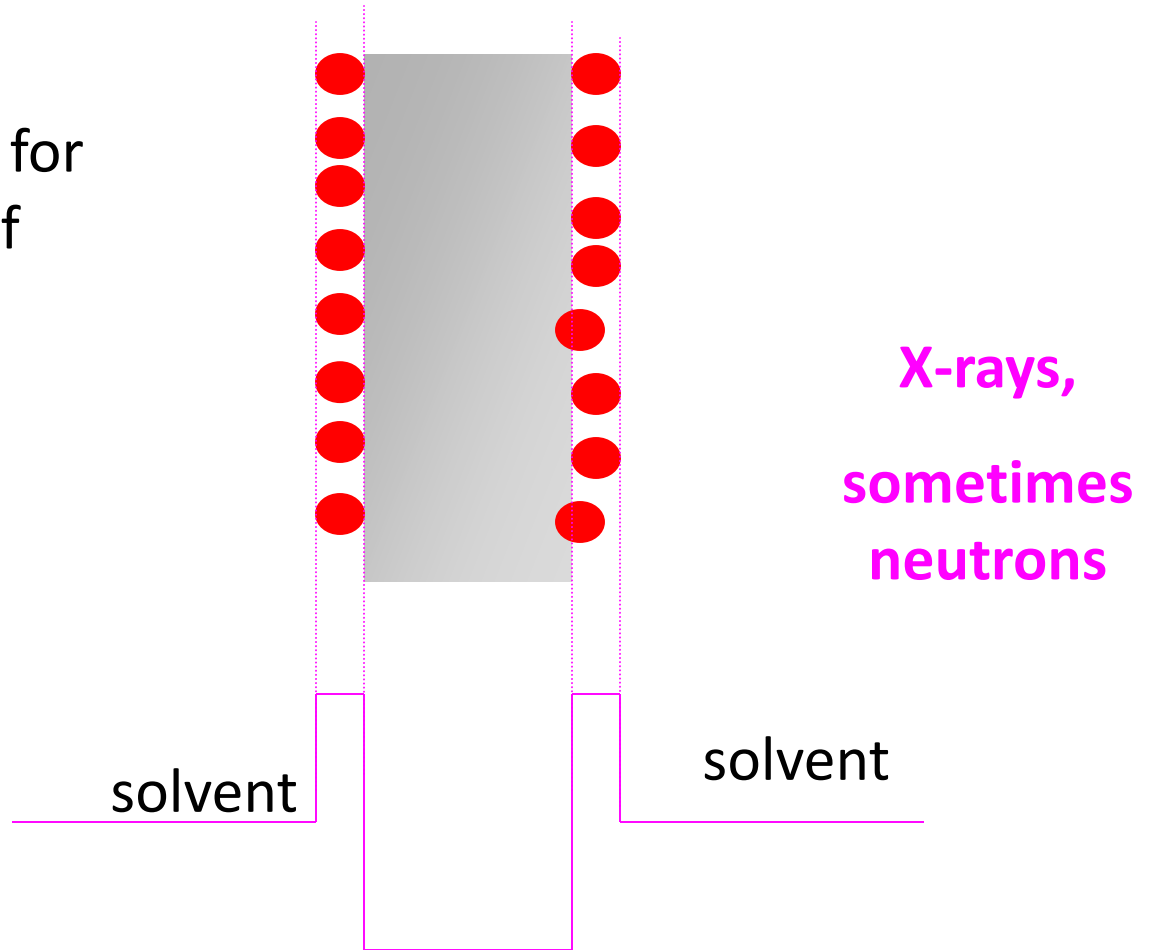
density $\rho = \sum b_i/V$

(sld)



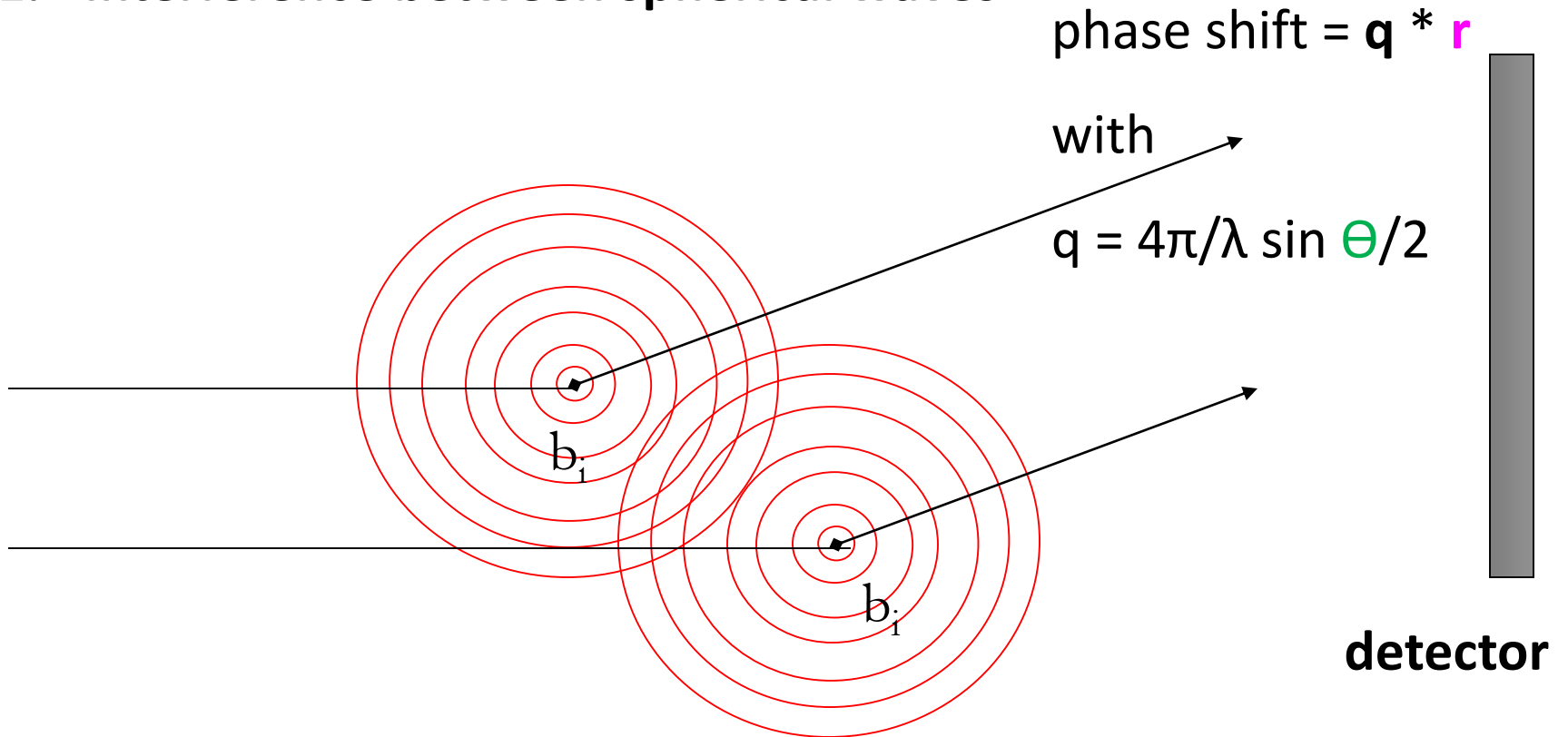
Contrast

Core shell models for
characterization of
hydrophilic shell.



Basic mechanism

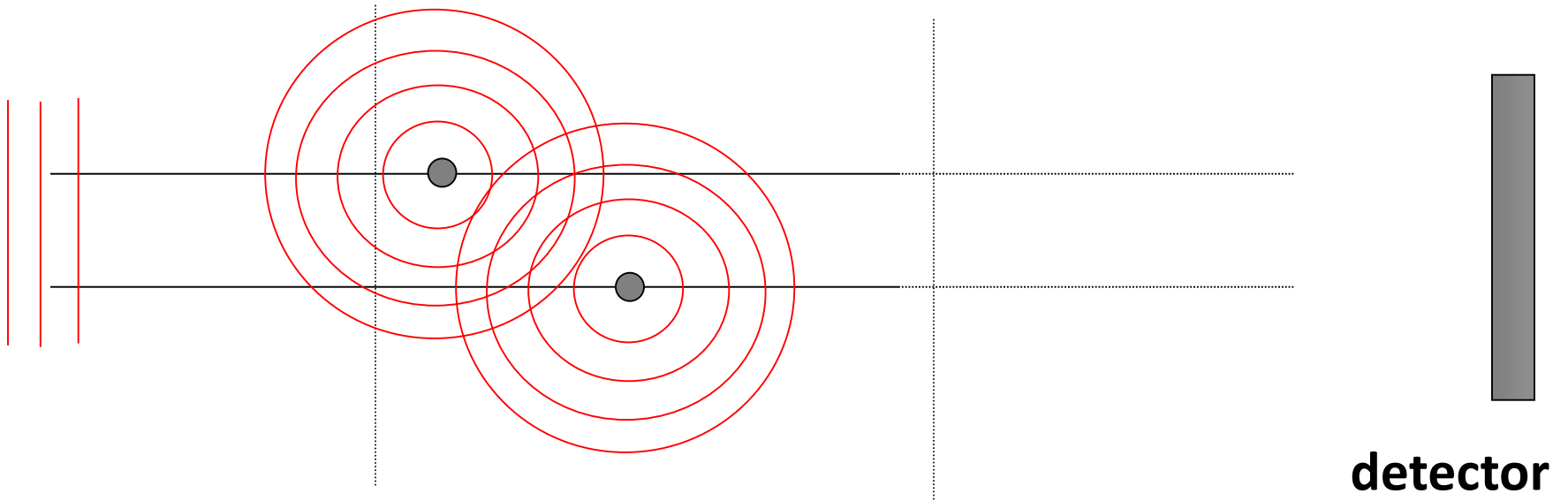
1. Interference between spherical waves



Small distances $\rightarrow$ large angles

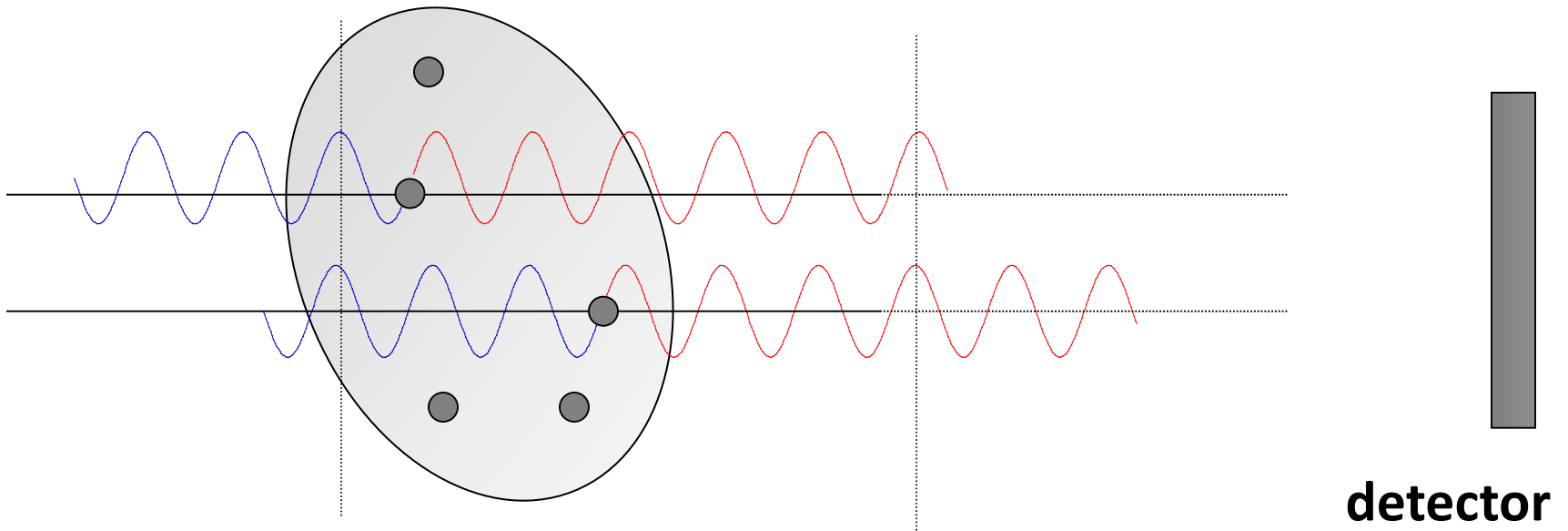
Large distances $\rightarrow$ small angles

2. Forward ($q=0$) scattering is additive



Basic mechanism

2. Forward ($q=0$) scattering is additive



No phase shift $\rightarrow$ constructive interference on detector

$$I(q \rightarrow 0) \propto \text{concentration} * \text{mass}$$



Basic mechanism

3. What mass is measured at $q > 0$?

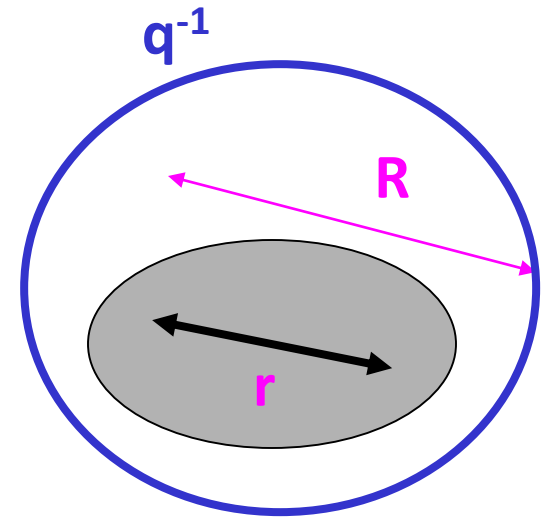
phase shift = $q * r$ with $q = 4\pi/\lambda \sin \Theta/2$

$$R < q^{-1}$$

$$\rightarrow r < q^{-1}$$

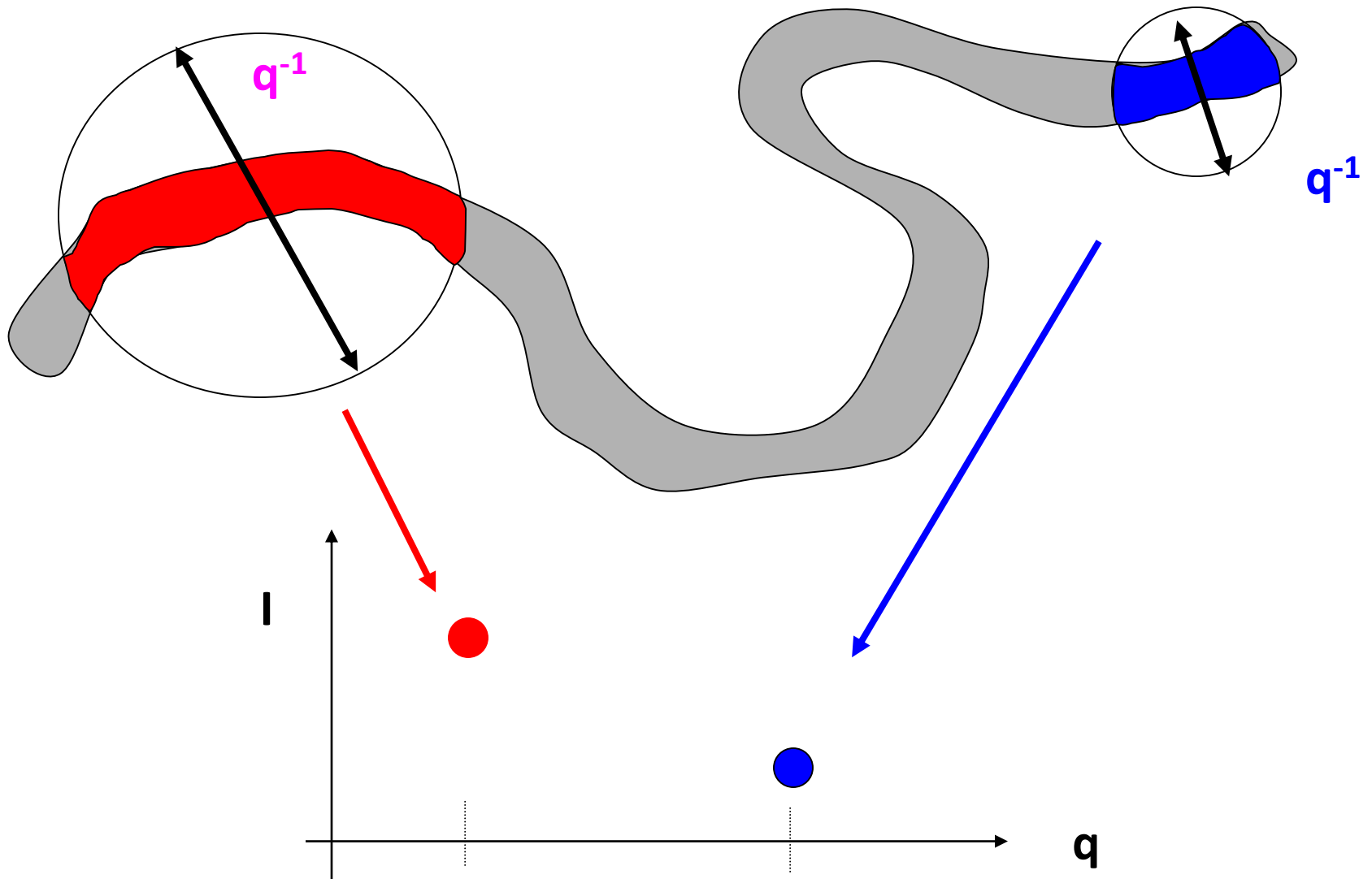
$$\rightarrow qr = \text{phase shift} \approx 0$$

$$\rightarrow I(q) = \text{mass inside sphere } q^{-1}$$



General scattering law

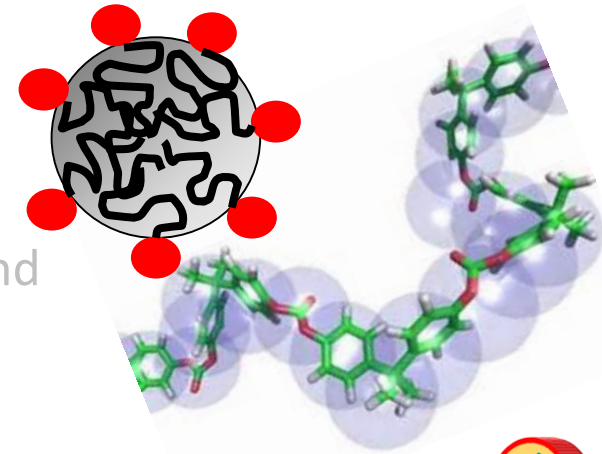
$I(q) \propto \text{mass inside sphere of radius } q^{-1}$



Outline

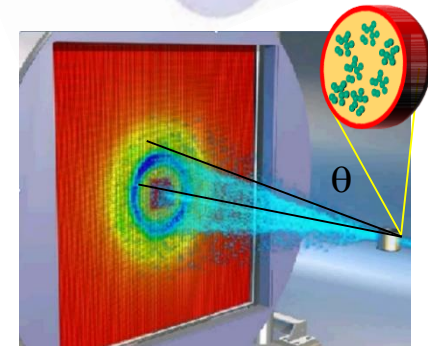
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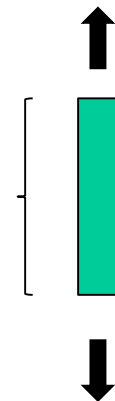
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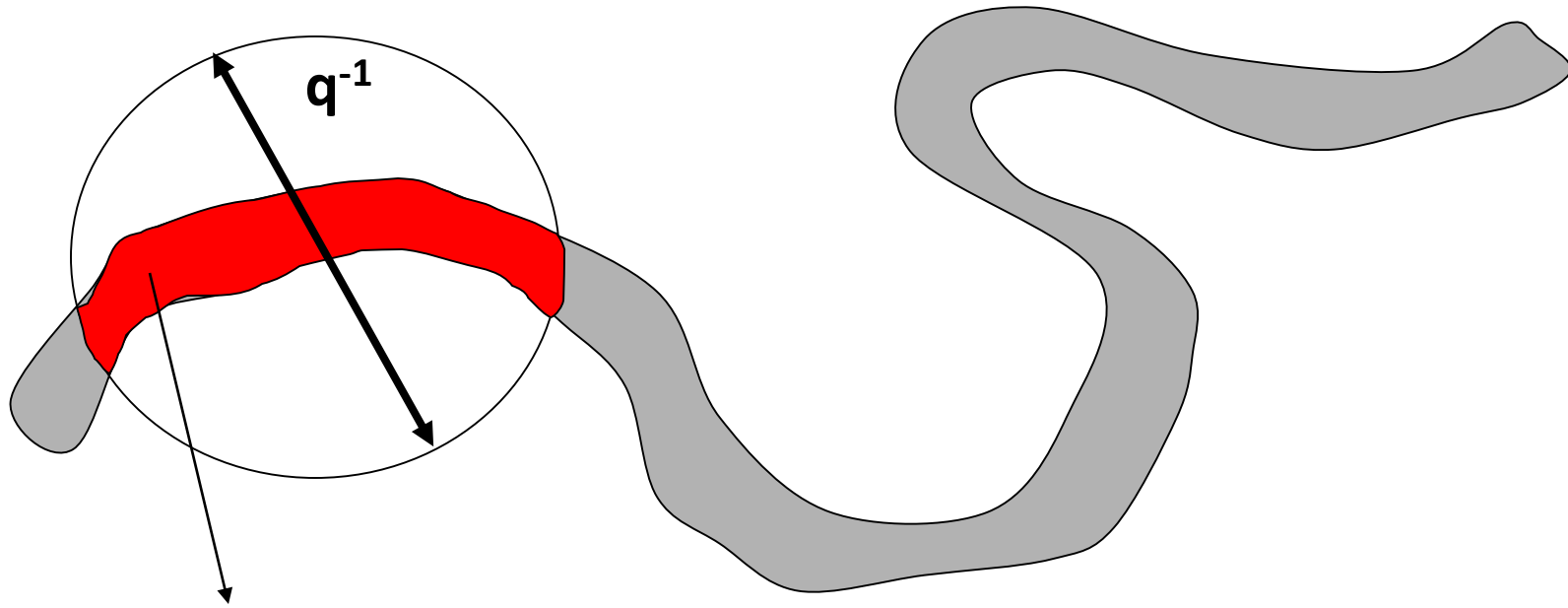
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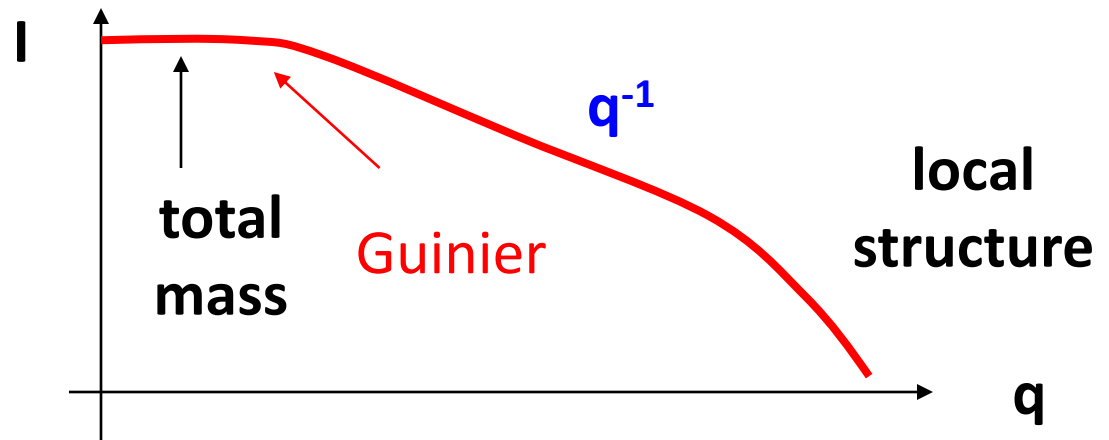


General scattering law: cylinders

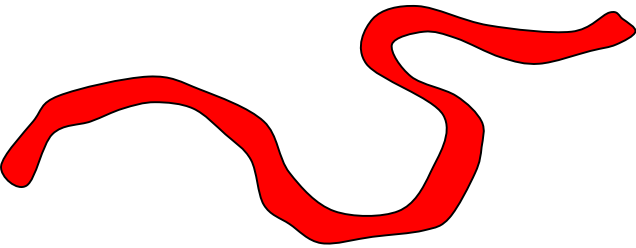


mass inside $\approx$ cylinder = Section x Length = $S q^{-1}$

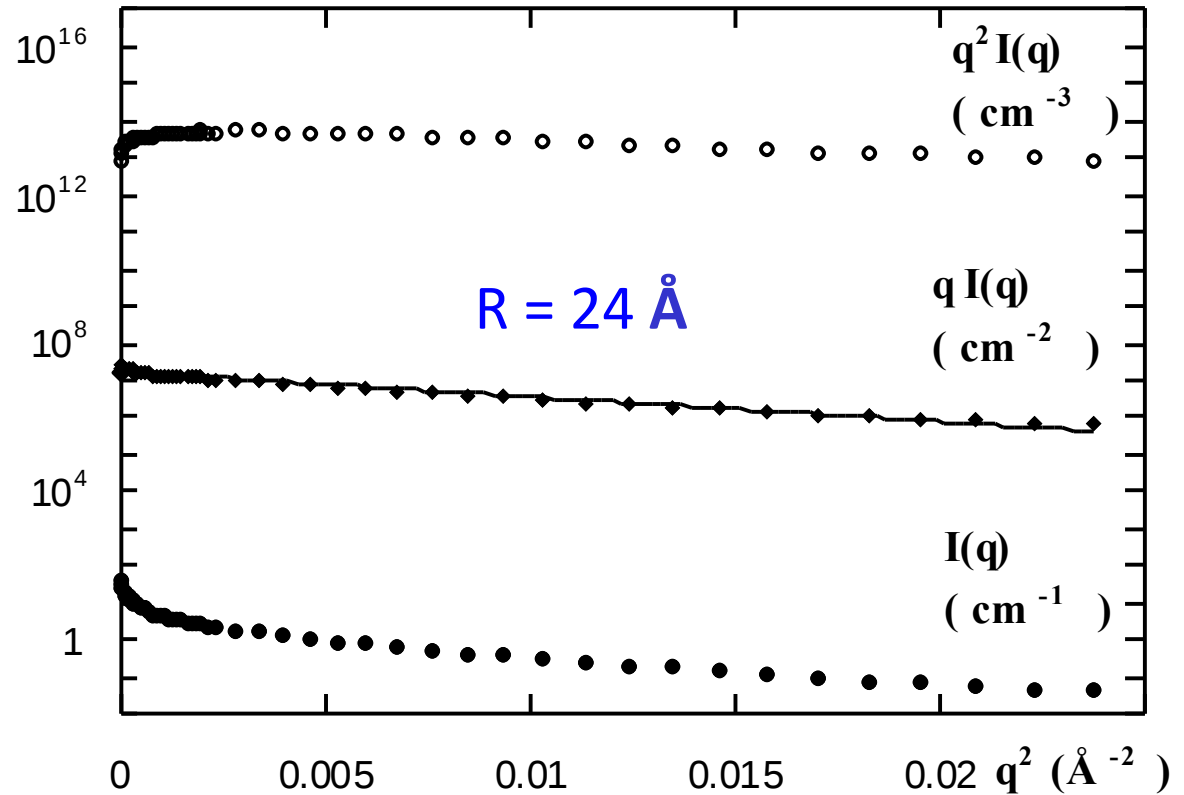
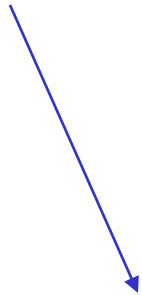
$$I(q) \propto \Phi S q^{-1}$$



Example of cylinders



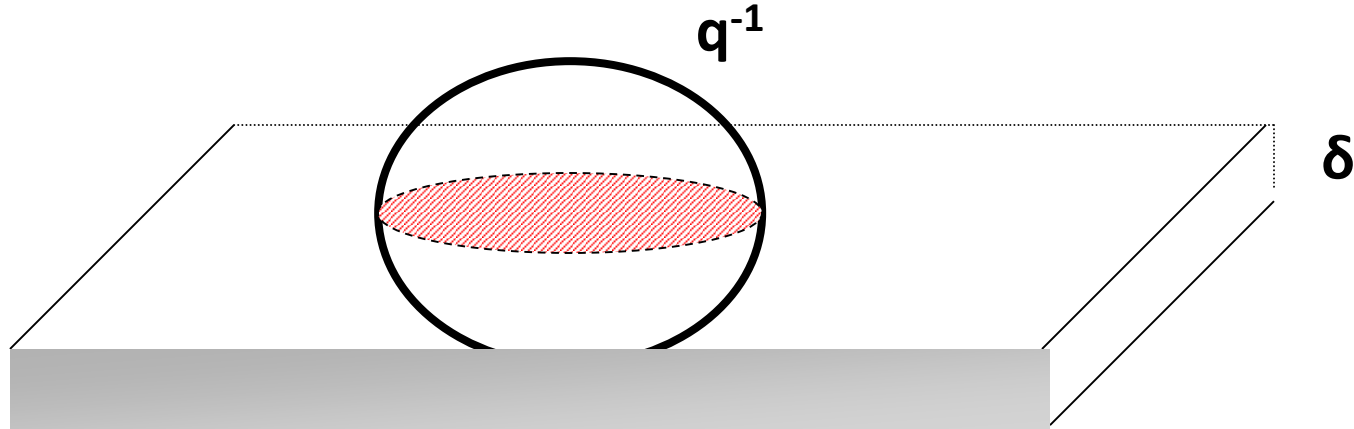
$$I(q) \propto \Phi S q^{-1}$$



Cylinders, small q : $q I(q) = \pi \Phi \Delta \rho^2 S \exp(-q^2 R^2/4)$

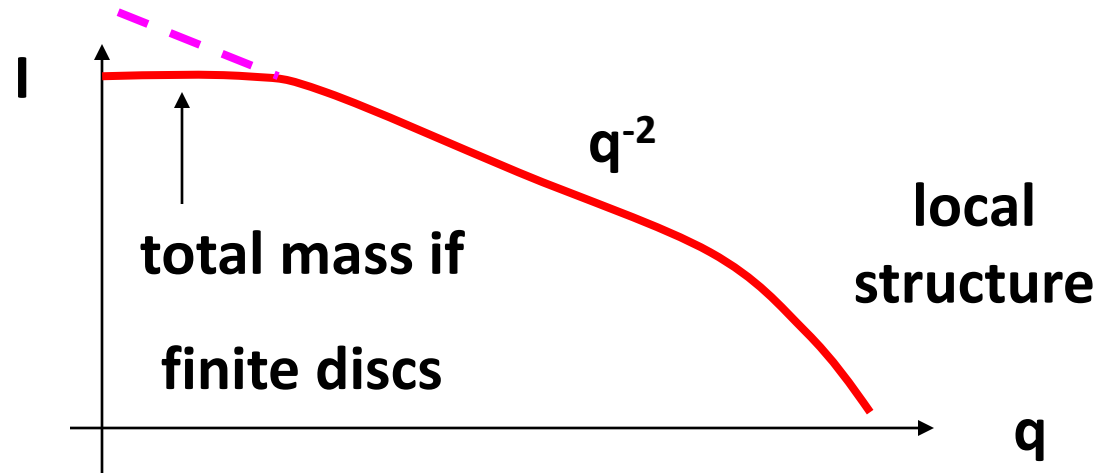
Guinier for cross section

General scattering law for flat bilayers



mass inside $\approx$ cylinder = thickness $\times$ surface = $\delta \pi q^{-2}$

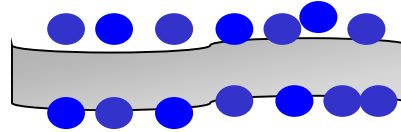
$$I(q) \propto \Phi \delta q^{-2}$$



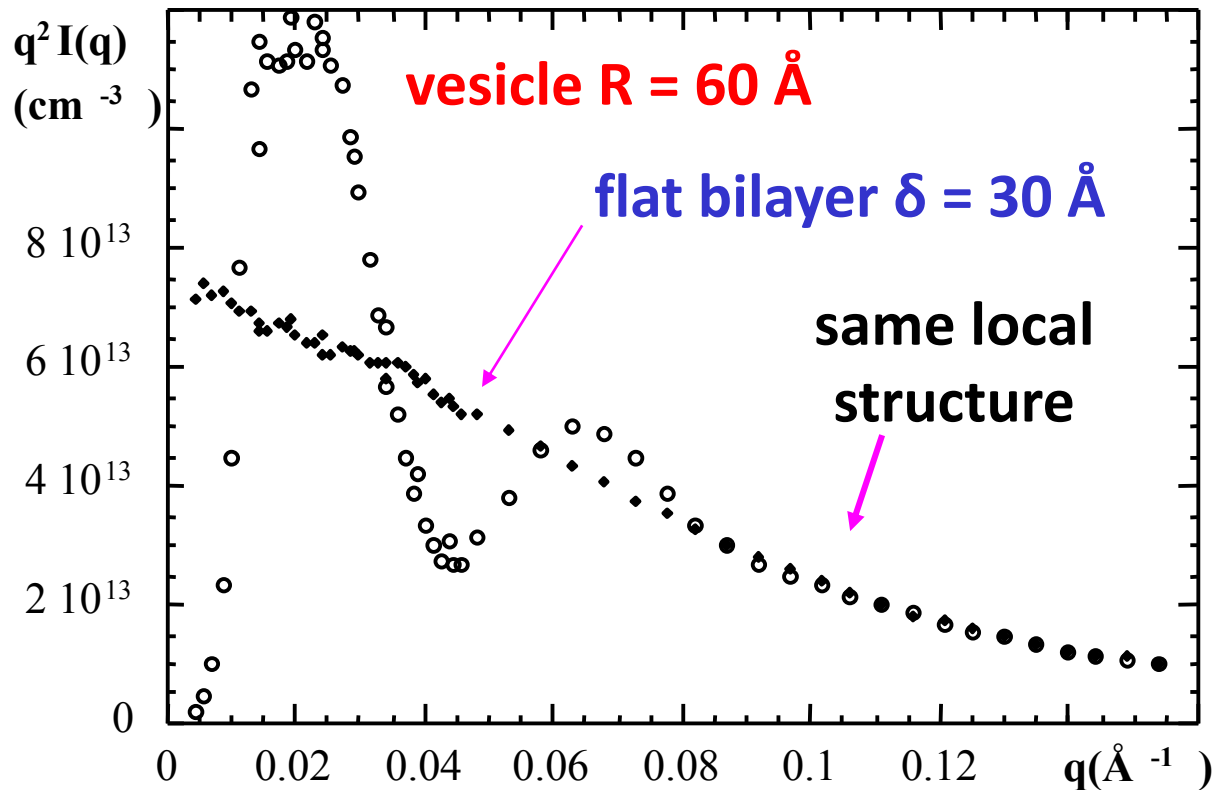
Example: flat vs. curved bilayers

flat bilayer

$$q^2 I(q) \propto \exp(-q^2 \delta^2 / 12)$$



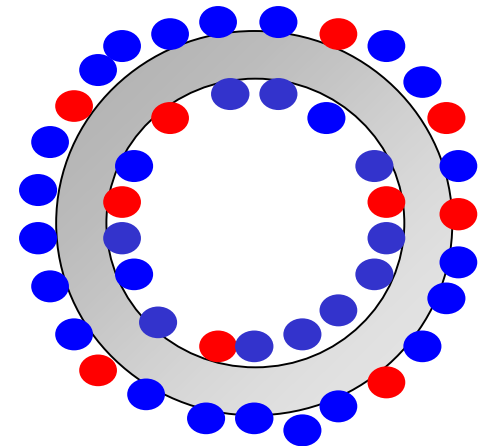
q^{-2} dependence



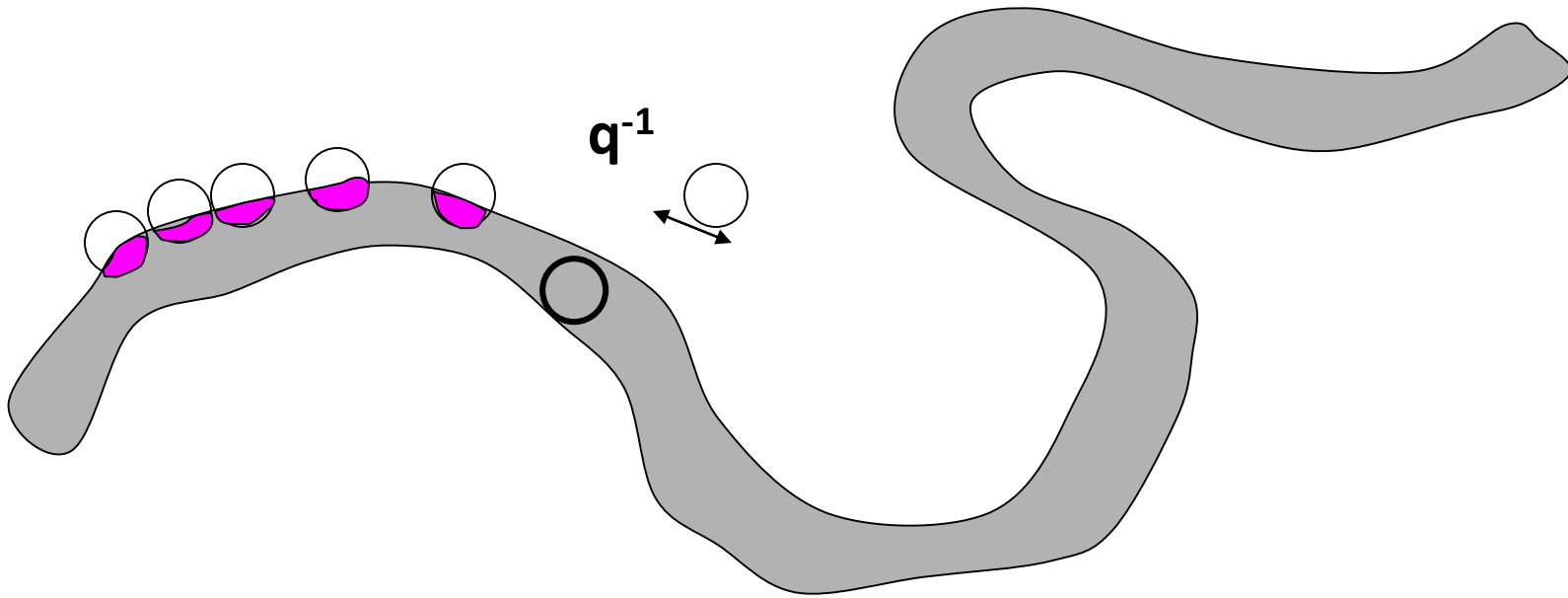
+ ionic surfactant

→ Radius

→ Helfrich κ 's



Smooth surfaces: Porod's law



1. Full or empty spheres do not contribute at $q > 0$.
2. Number of half empty spheres = surface / $\pi R^2 \propto S q^2$
3. Each sphere on surface contributes: mass $\propto R^3 \propto q^{-3}$

=> Porod law for smooth surfaces: $I \propto \text{number} \times \text{mass}^2$

$$I \propto A/q^4 \quad (A \text{ gives specific surface } S/V)$$

Fractal surfaces: modified Porod's law

B. Mandelbrot: how long is the coast of Britain?

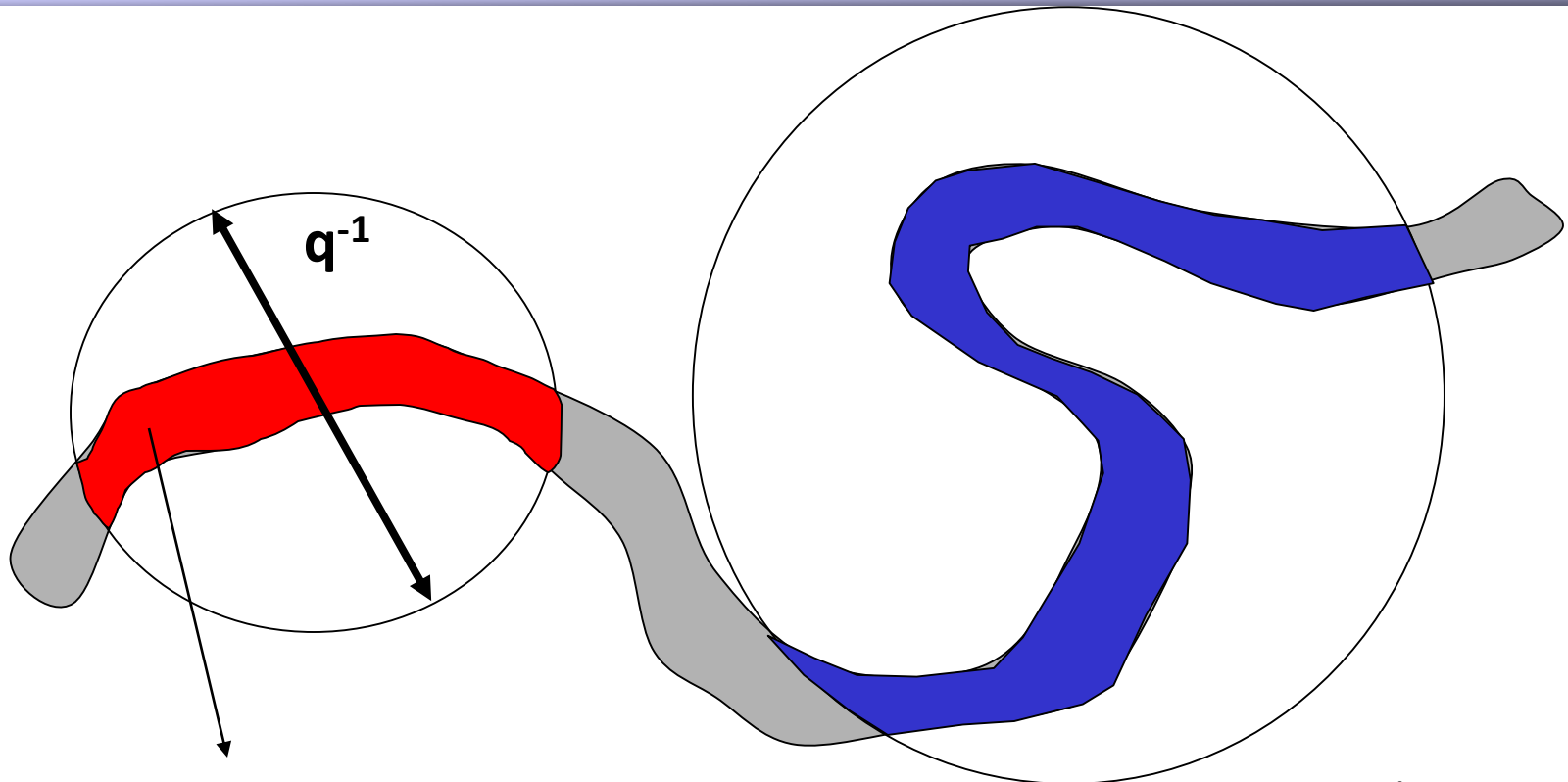


1. Full or empty spheres do not contribute at $q > 0$.
2. Number of half empty spheres $\propto q^D$
3. Each sphere on surface contributes: mass $\propto R^3 \propto q^{-3}$

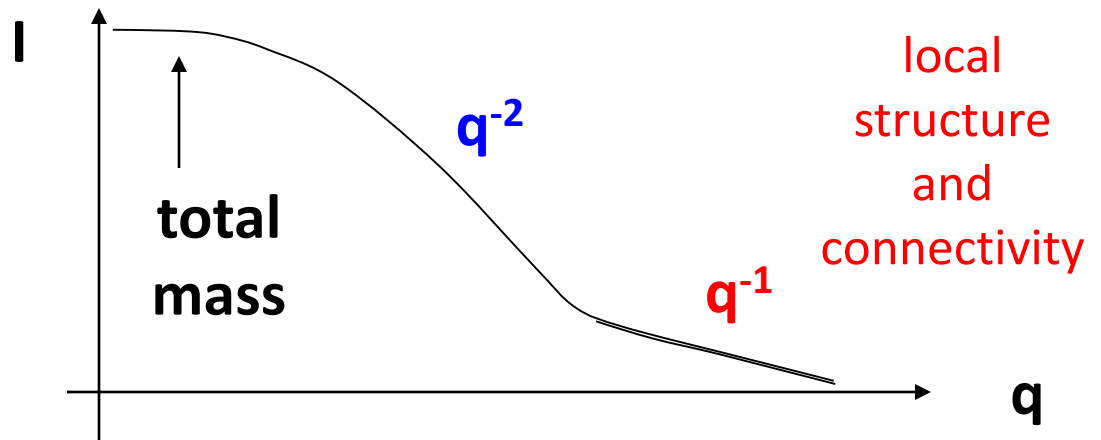
=> Porod law for fractal surfaces: $I \propto \text{number} \times \text{mass}^2$

$$I \propto A/q^{6-D}$$

Conformation of polymer chains

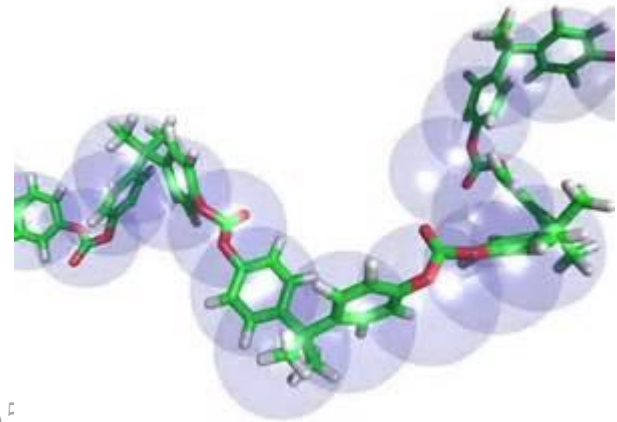


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Conformation of polymer chains

Linear polymer chain (e.g. PEO, PE, PS):



 In (theta-)solvent: $R \approx 15 \text{ nm}$

- Number of conformations: $3^{10^4} \approx 10^5$
- One picosec/conformation: (much) longer than age of universe

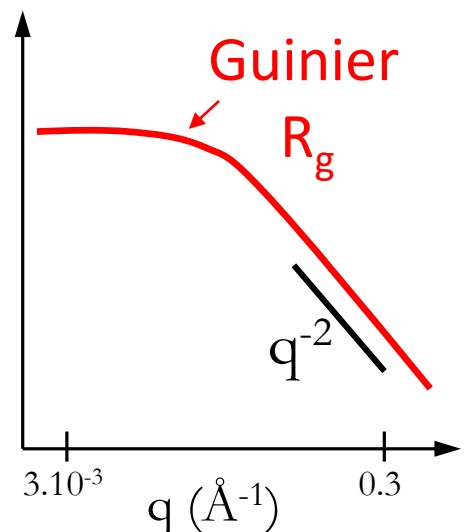
→ statistical description: $R_g = a N^{1/2} \sim M^{1/2}$

→ $I \sim M \sim R_g^2 \sim q^{-2}$

Debye function of Gaussian chains:

$$P_{\text{Debye}}(q) = \frac{2}{q^4 R_g^4} \left(e^{-q^2 R_g^2} - 1 + q^2 R_g^2 \right)$$

Now, q^{-2} is chain or sheet?



Conformation of polymer chains

Generalized Gaussian coil

Arbitrary conformation exponent:

→ statistical description: $\mathbf{R}_g = a N^\nu$

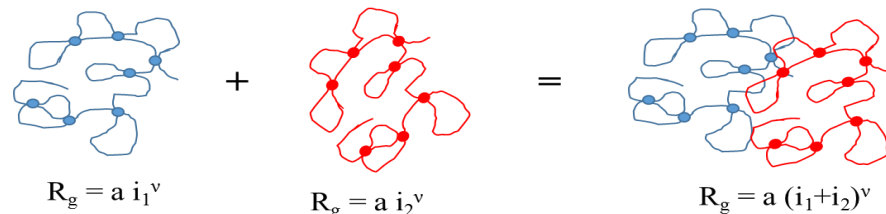
→ fractal dimension: $d_f = 1/\nu$
expresses **solvent** conditions

$$P(q, R_g) = \left[\left(\frac{1}{\nu U^{2\nu}} \right) \gamma \left(\frac{1}{2\nu}, U \right) - \left(\frac{1}{\nu U^{\frac{1}{\nu}}} \right) \gamma \left(\frac{1}{\nu}, U \right) \right]$$

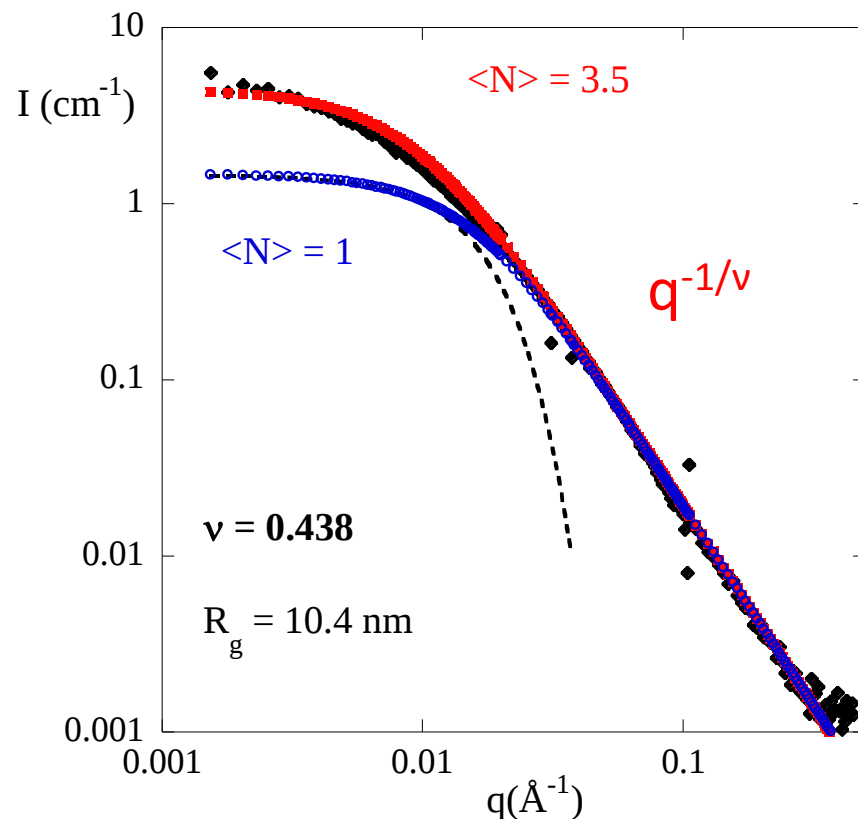
with

$$U = (2\nu + 1) \cdot (2\nu + 2) \cdot \frac{(qR_g)^2}{6}$$

$$\gamma(a, b) = \int_0^b t^{a-1} e^{-t} dt$$



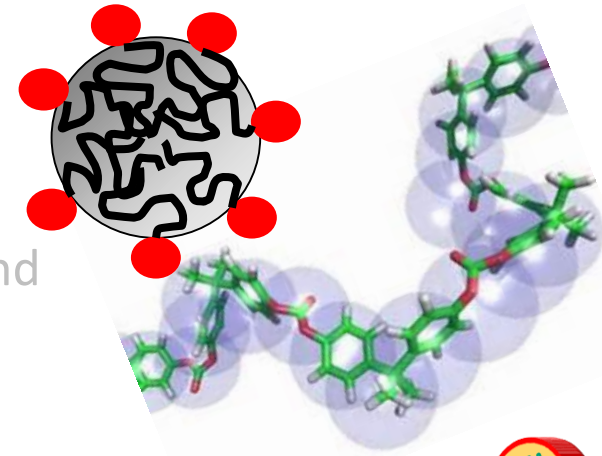
*'Single-chain NP',
Arbe, Colmenero, JO*



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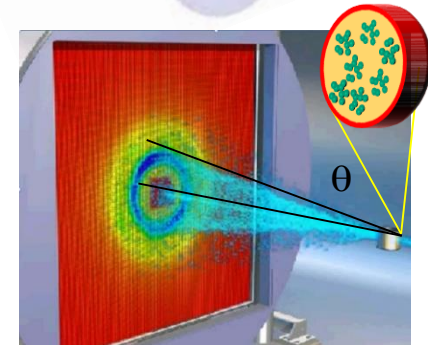
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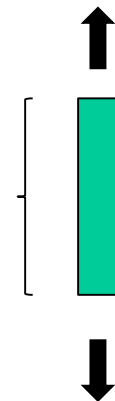
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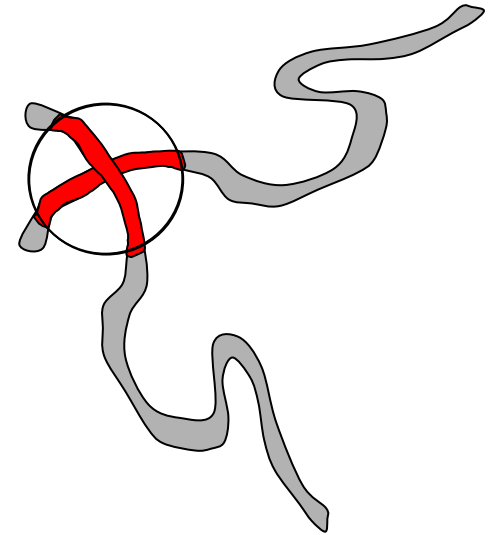
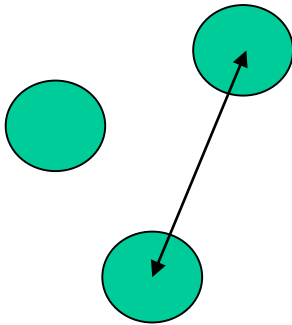
$$L = \lambda L_0$$



Interactions

From single (finite-size) particle to many:

Interactions easiest with spheres



Spheres described by **form factor** $P(q)$,
interactions by **structure factor** $S(q)$

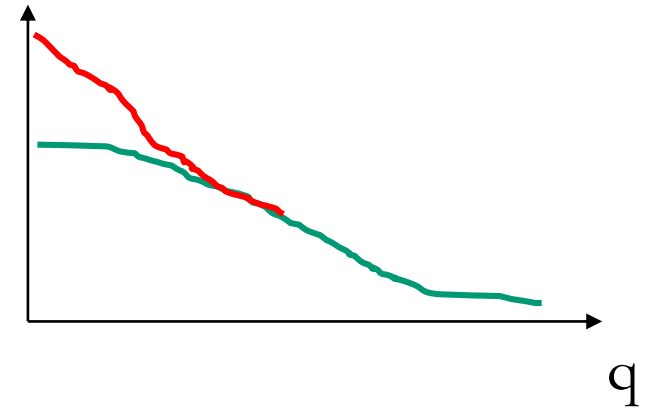
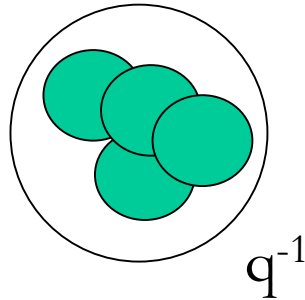
Only for identical objects of spherical symmetry:

$$I(q) = I_o P(q) S(q)$$

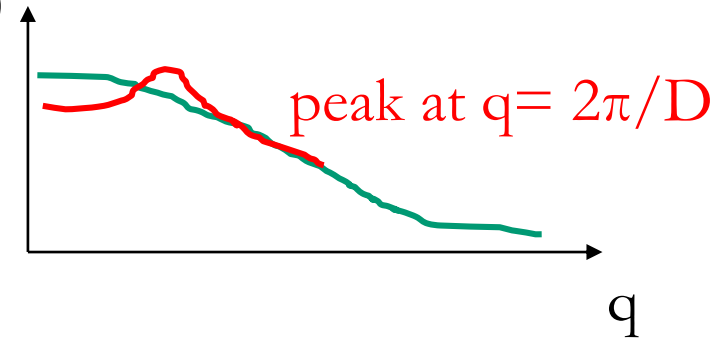
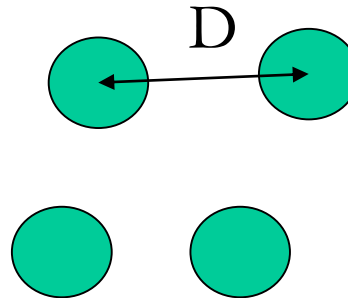
What does $S(q)$ do to
scattered intensity?

Interactions and structure factor $S(q)$

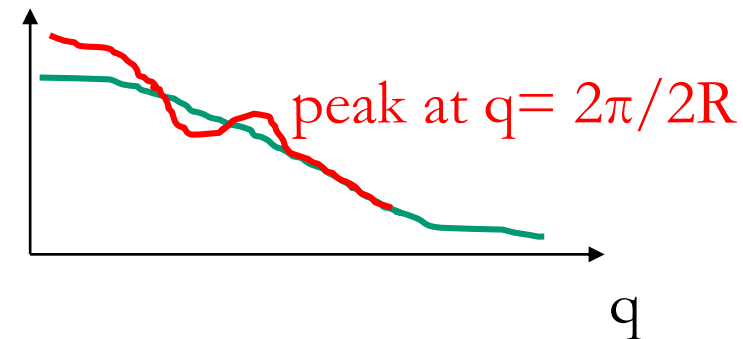
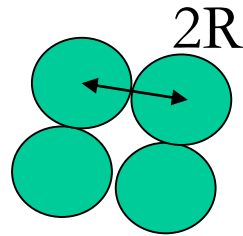
Attractive interactions:
mass increases in
 q^{-1} sphere



Repulsive interactions:

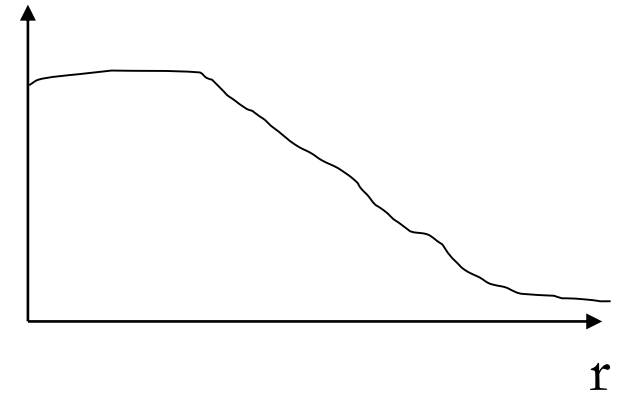
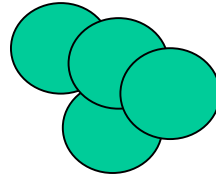


Both:

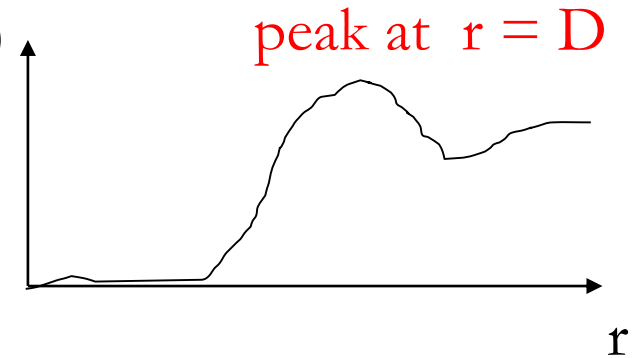
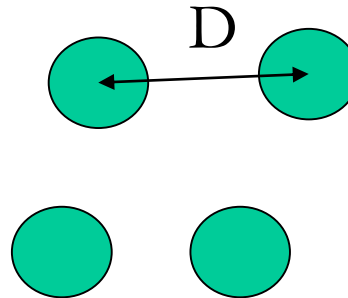


Interactions and pair correlation function $g(r)$

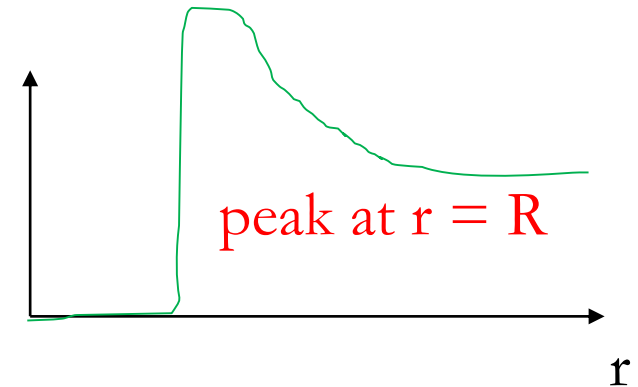
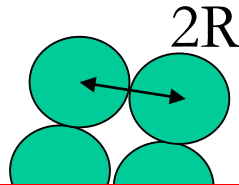
Attractive (soft) interactions:



Repulsive interactions:



Both:

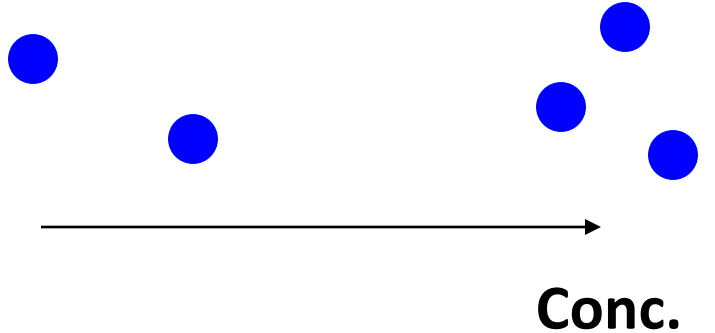


$g(r)$ is the Fourier transform of $S(q)$

$$S(q) = 1 + 4\pi \frac{N}{V} \int_0^{\infty} [g(R) - 1] R^2 \frac{\sin qR}{qR} dR$$

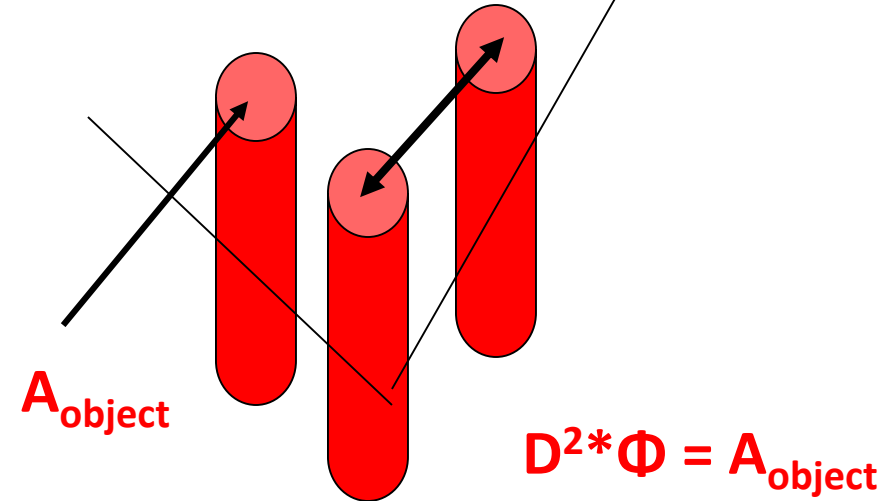
Interactions in practice: dilution laws to follow structure peaks

Globular objects

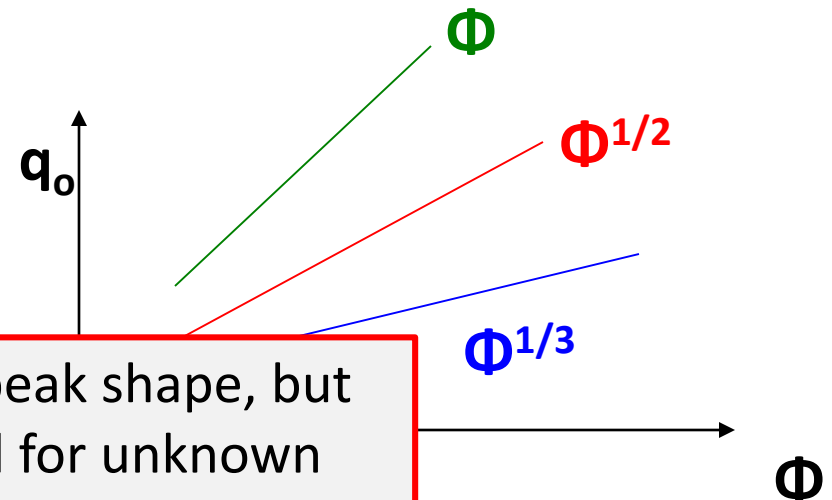
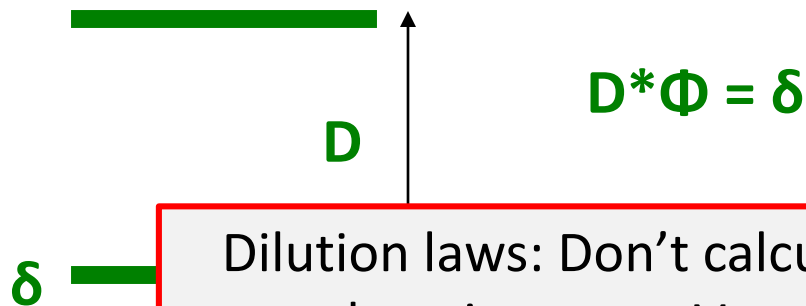


Cubic model: $D^3 * \Phi = V_{\text{object}}$

Ordered Cylinders

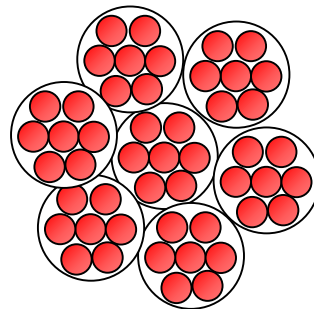
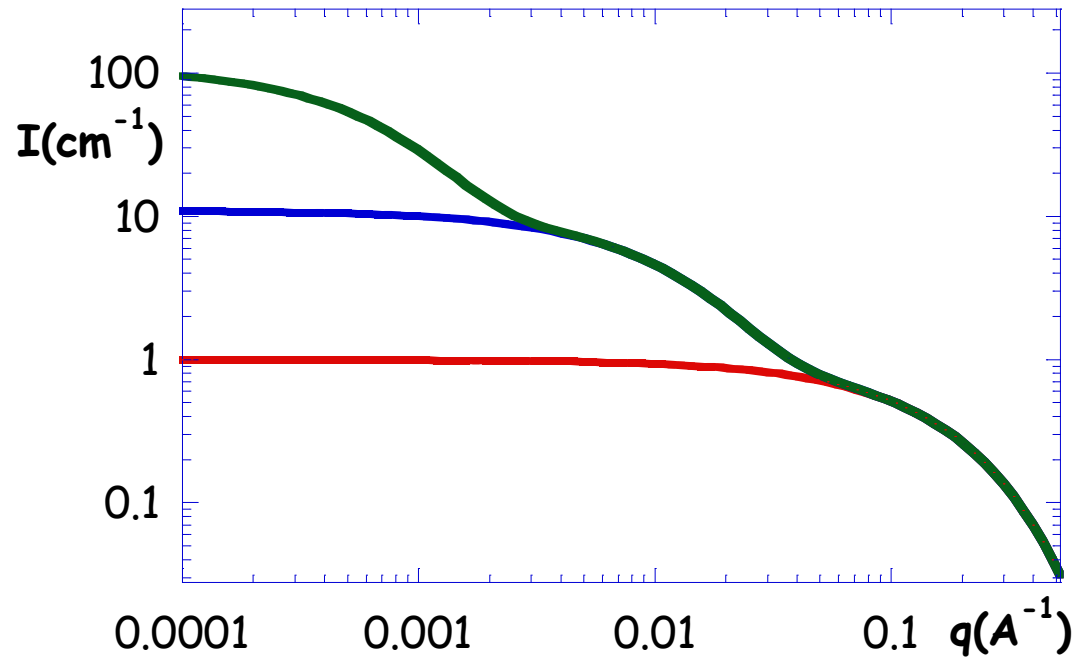


Flat bilayers

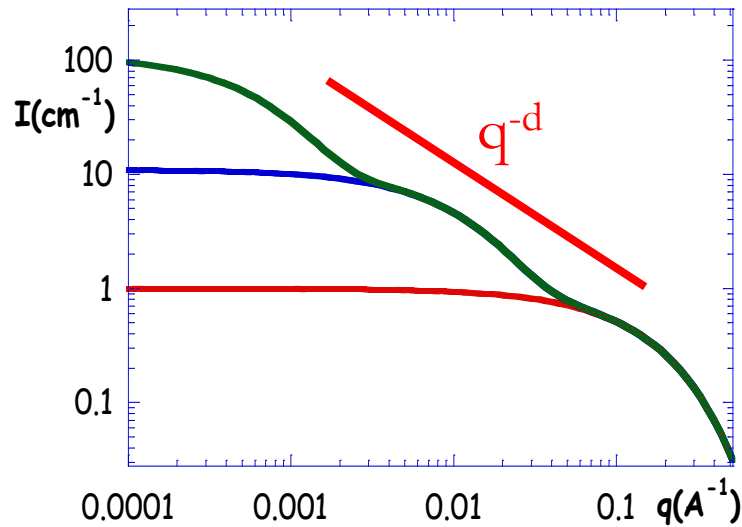


Dilution laws: Don't calculate peak shape, but see how it moves. Very useful for unknown structures (cf. microemulsions).

Scattering from hierarchical systems: nanoparticle aggregates

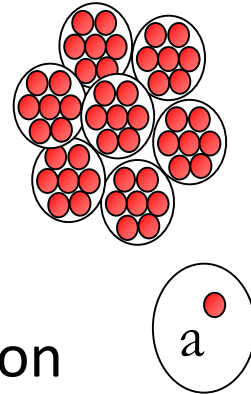


Scattering from hierarchical systems: nanoparticle aggregates



Fractals:

- self-similar
- $N = (R/a)^d$
- d is the fractal dimension

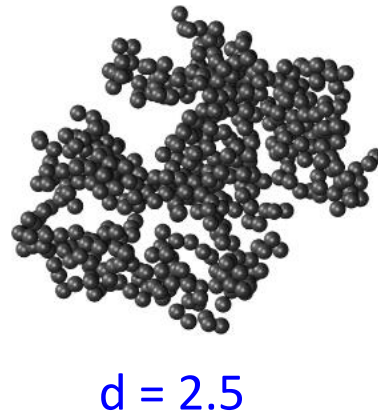
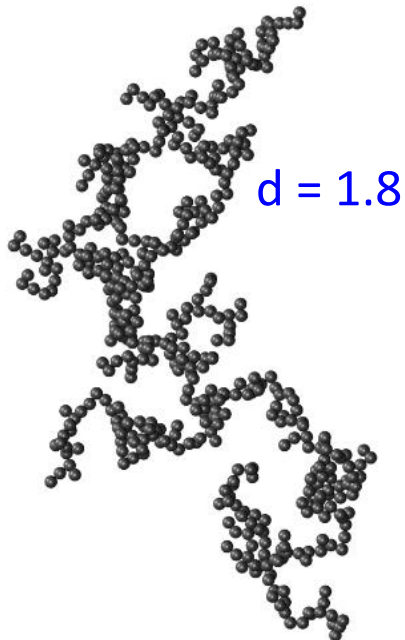


Scattering law:

- Mass in sphere of radius q^{-1}
- $N = (R/a)^d$
- **$I(q) \sim \text{mass} \sim N \sim 1/(qa)^d \sim 1/q^d$**

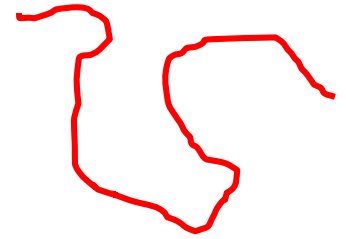
Our examples:

- Cylinder q^{-1}
- Sheet or Gaussian polymer q^{-2}
- Chain in good solvent: $q^{-1/\nu}$
- Surface q^{-4} (or surface fractal)



Scattering of polymer networks

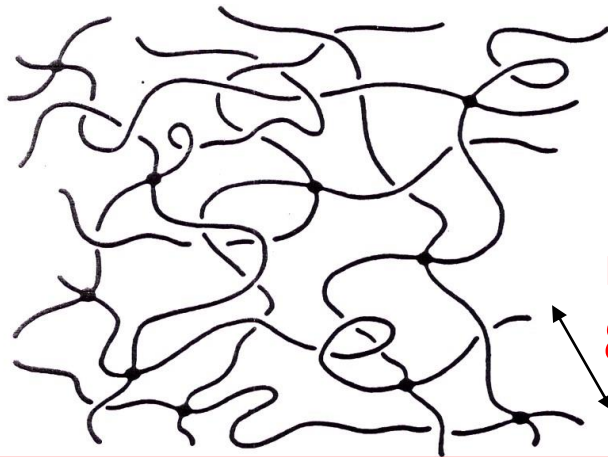
- Single chain: $g(r) = 1/r$ and finite size R_g
 $\Rightarrow$ Debye function in q^{-2} , I_0 = chain mass



- $g(r)$ of single chain with cut-off: $g(r) = 1/r \exp(-r/\xi)$

Ornstein-Zernike (OZ) $I(q) = \frac{I_0}{1+(q\xi)^2}$

I_0 = fluctuations



mesh size

ξ

OZ and Debye look similar, interpretation different

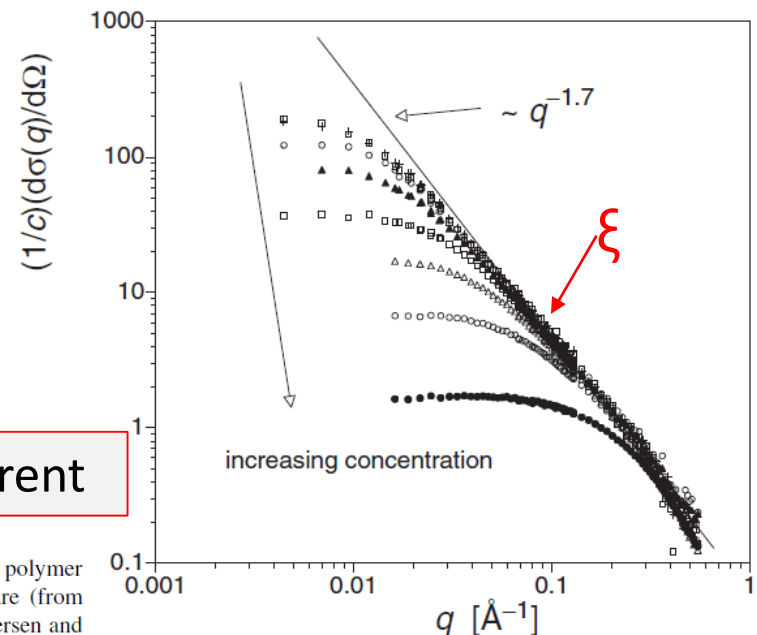
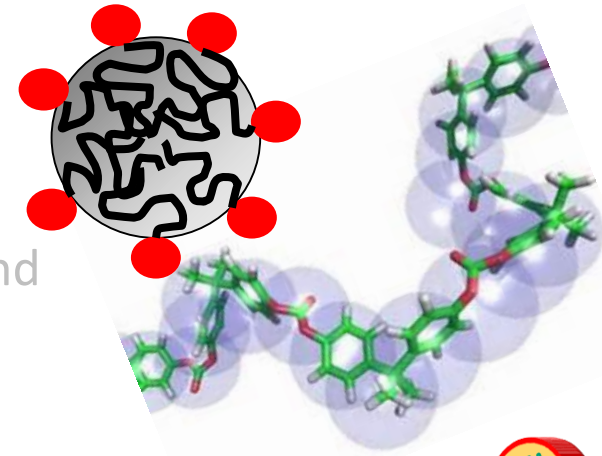


Fig. 20. Normalized scattering intensity $I(q)/c$ as a function of the scattering vector q for different polymer concentrations c for polystyrene in deuterated toluene and $M_w = 120,000$ g/mol. The concentrations are (from below) $c = 0.27, 0.11, 0.054, 0.028, 0.011, 0.0052, 0.0021$ and 0.0013 g/ml. The data are taken from Pedersen and Schurtenberger (1999).

Outline

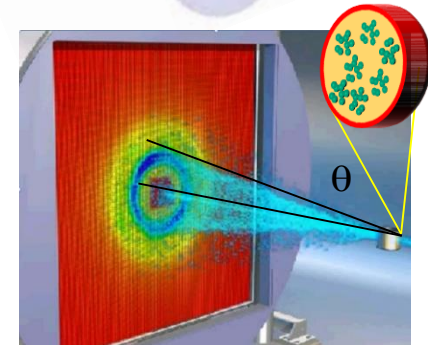
1) Soft matter as microstructured systems

- Surfactant self-assembly
- Polymer systems: molecules, networks, particles and nanocomposites



2) Structural analysis by small-angle scattering

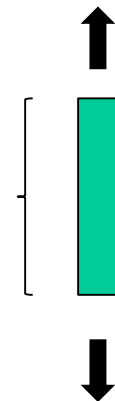
- Principles: contrast, scattering process
- Shape analysis, a 'math-free' Fourier transform
- Applications: micelles, bilayers, polymers, surfaces, aggregates
- Interactions and pair correlation



3) Scattering under deformation

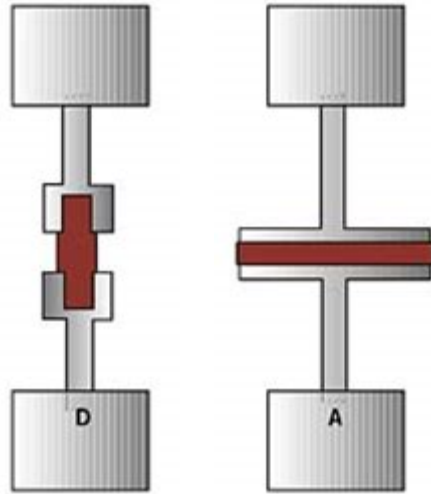
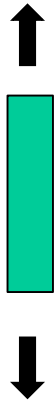
- Experiments and geometries
- Affine deformation and networks

$$L = \lambda L_0$$



Scattering of samples under deformation

Solids



Torsion, shear

Uniaxial
strain

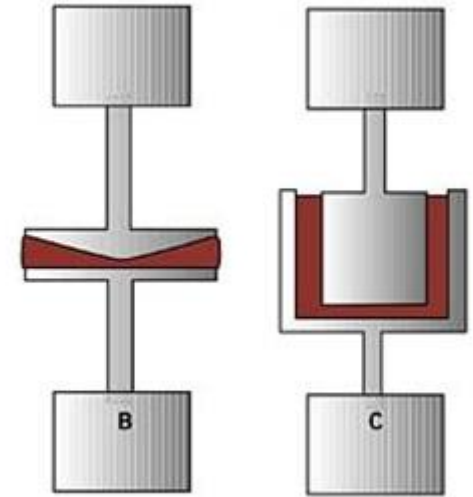
$$\lambda = \varepsilon + 1 = L/L_0$$

macroscopic deformation



elastomers, rubber, gels:
polymer networks

Liquids



Cone-plate, Couette

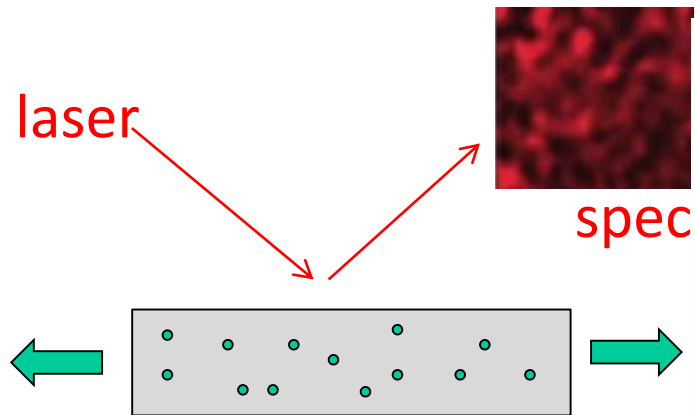
γ



polymer or surfactant
solutions, soft gels

Scattering experiments

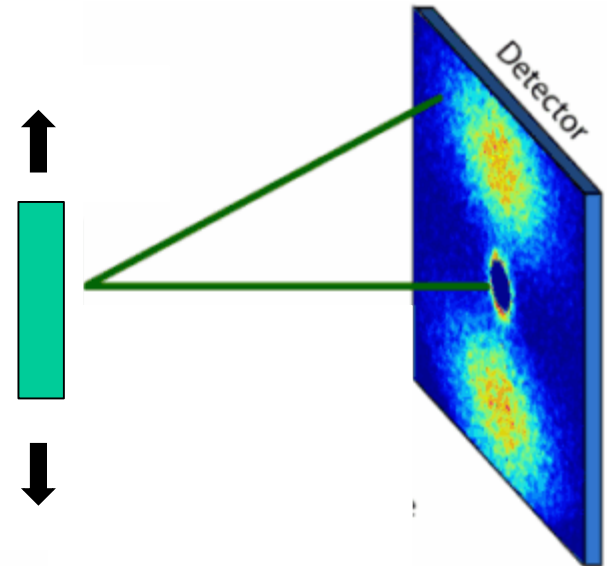
e.g. diffusive wave spectroscopy (DWS) in backscattering



tracer NPs or ... PNC

No idea on the structure!
Back-and-forth (echo) tells you, if same structure is retrieved after motion (with L. Cipelletti, U Montpellier).

Small-angle scattering (SAS)
→ single scattering event



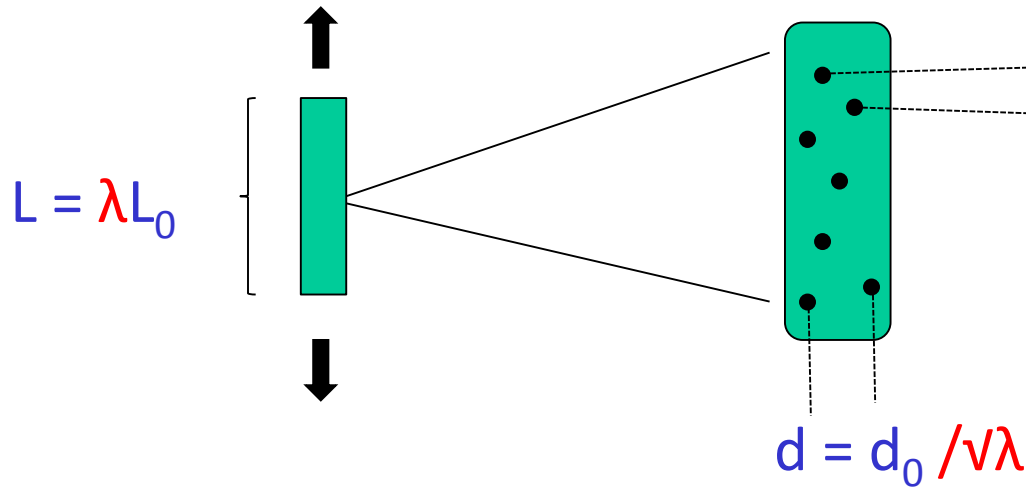
$I(q_x, q_y)$ instead of $I(q)$ gives micro-structure in different directions.

Different scattering experiments and geometries give different information

Affine deformation

Macroscopic strain

$$\lambda = L/L_0$$



What about the other two directions?

In case of volume conservation and symmetry: $V = L_x L_y L_z = L_{0x} L_{0y} L_{0z}$

$$V = \lambda_x L_{0x} \lambda_y L_{0y} \lambda_z L_{0z}$$

$$\lambda_x \lambda_y \lambda_z = 1$$



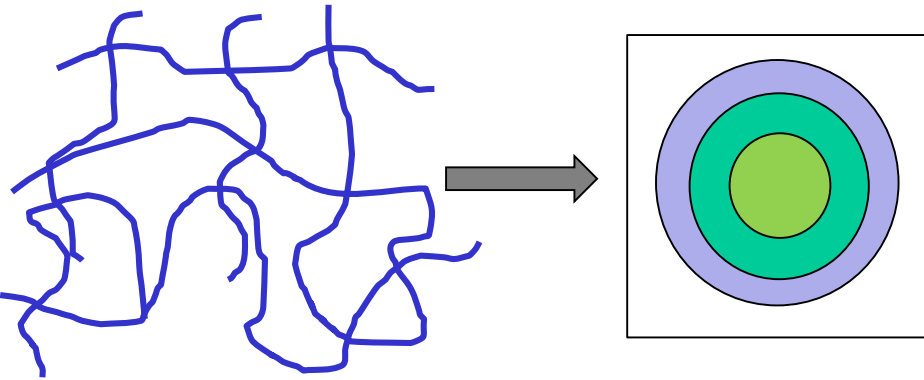
Uniaxial strain in z-direction:

$$\lambda_z = \lambda$$

$$\lambda_x = \lambda_y = 1/\sqrt{\lambda}$$

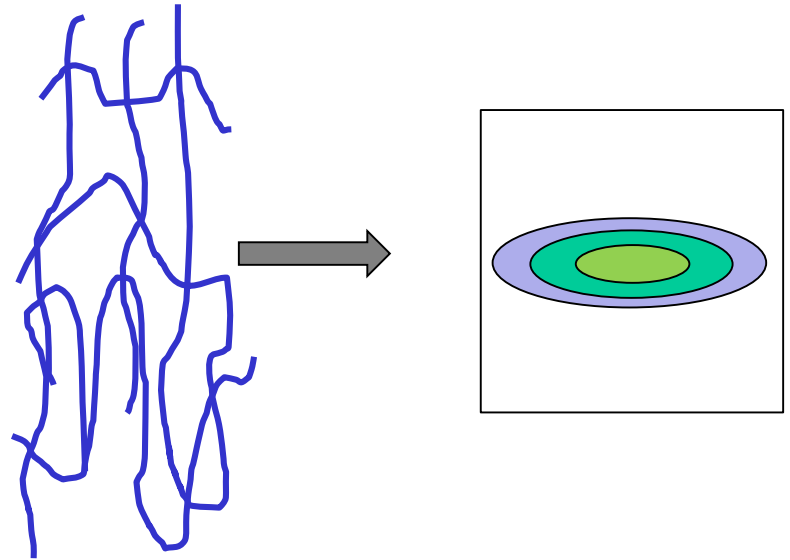
Affine deformation and scattering

Initial isotropic structure



Radius of ring: q_0

Deformation: $\lambda, 1/\sqrt{\lambda}$



Ellipse : affine deformation of ring:

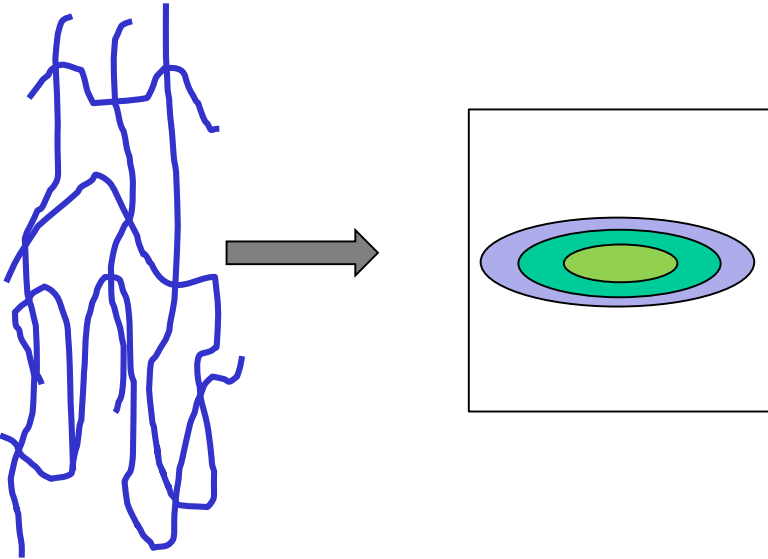
=> Follow deformation
on local scale!

$$q_z = q_0 / \lambda$$

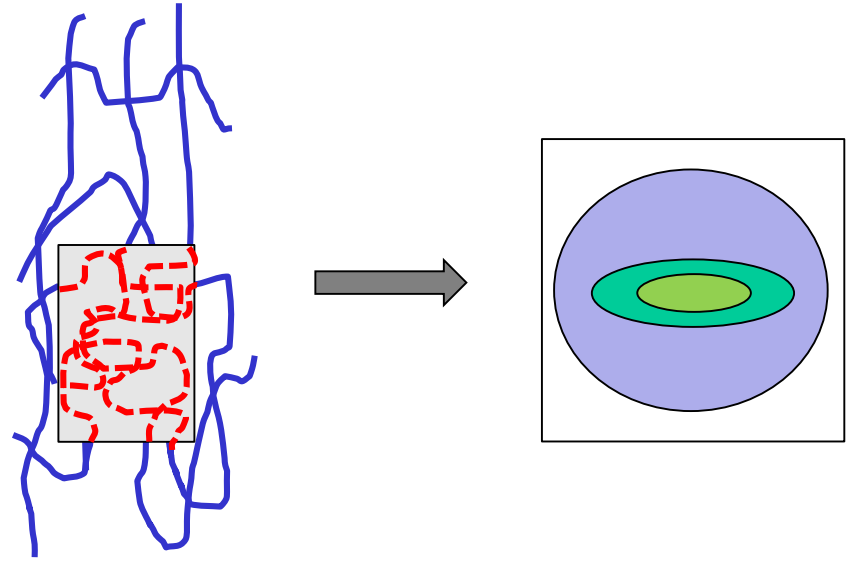
$$q_x = q_0 \sqrt{\lambda}$$

Partially affine: Observation of relaxation

Step-strain deformation: λ , $1/\sqrt{\lambda}$



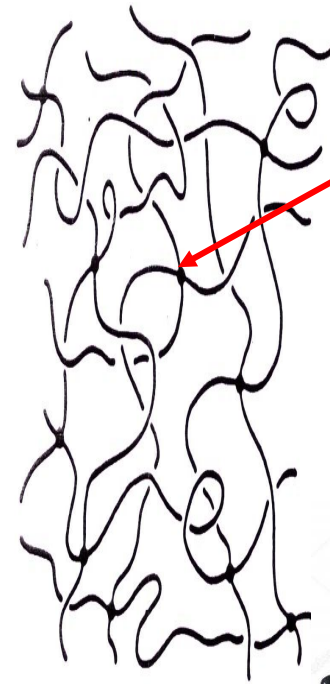
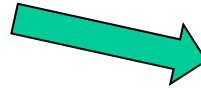
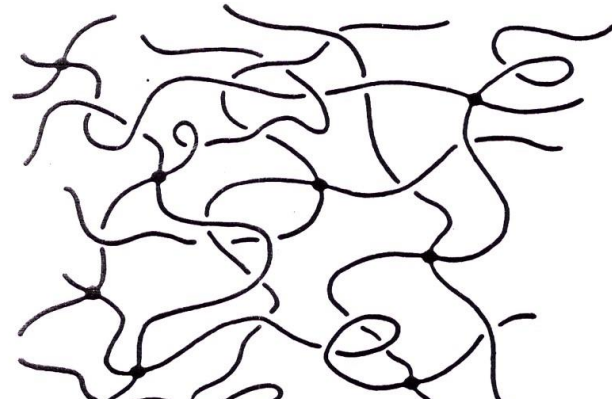
Relaxation at constant strain



'isotropized'

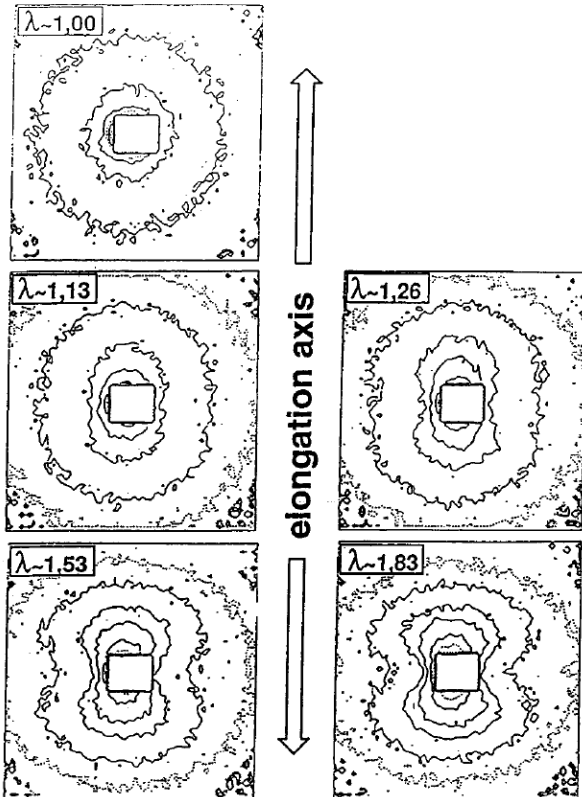
- ⇒ Determine q -vector (= typical size) delimiting affineness.
- ⇒ Gives scale of spatial reorganization (with time).

Studies of network deformation



Displacement of junctions?

Network theories



Macromolecules **1996**, *29*, 5574–5584

Small-Angle Neutron Scattering Study of Swollen Elongated Gels: Butterfly Patterns

E. Mendes,^{*,†,‡} R. Oeser,[§] C. Hayes,^{†,§} F. Boué,^{||} and J. Bastide^{⊥,Δ}

Figure 3. Isointensity curves as a function of the elongation ratio, λ , for the sample at swelling ratio $Q = 23$.

Studies of network deformation

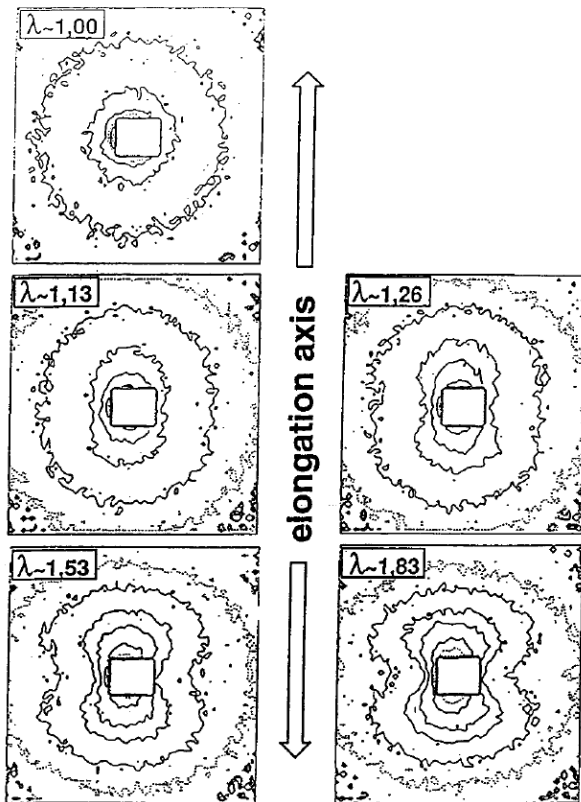


Figure 3. Isointensity curves as a function of the elongation ratio, λ , for the sample at swelling ratio $Q = 23$.

Macromolecules **1996**, *29*, 5574–5584

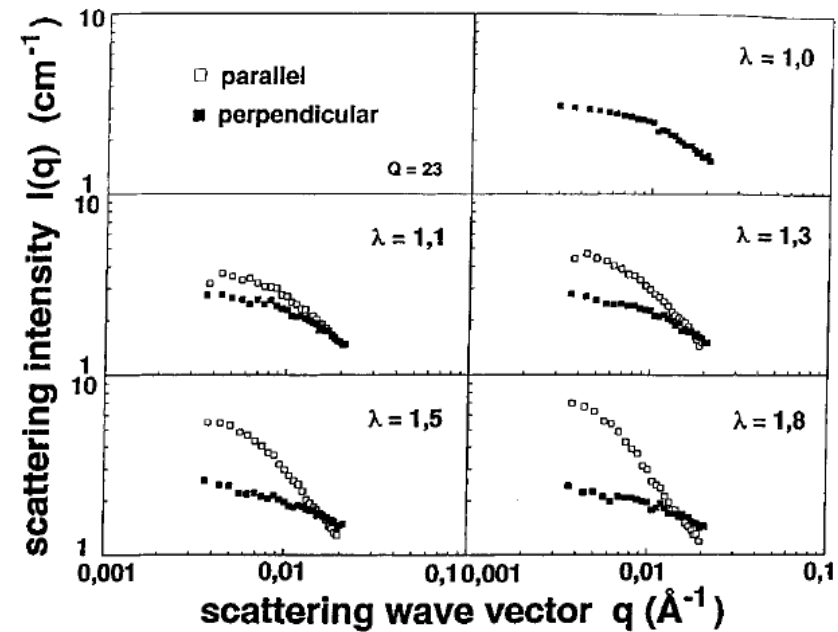


Figure 4. Scattered intensity, $I(q)$ in the parallel and in the perpendicular directions as a function of q , for different elongation ratios, λ . A log–log representation is used. The swelling ratio is $Q = 23$.

OZ: Extract screening length and I_0 (fluctuations) and compare to models (overestimate).

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Studies of network deformation: relaxation

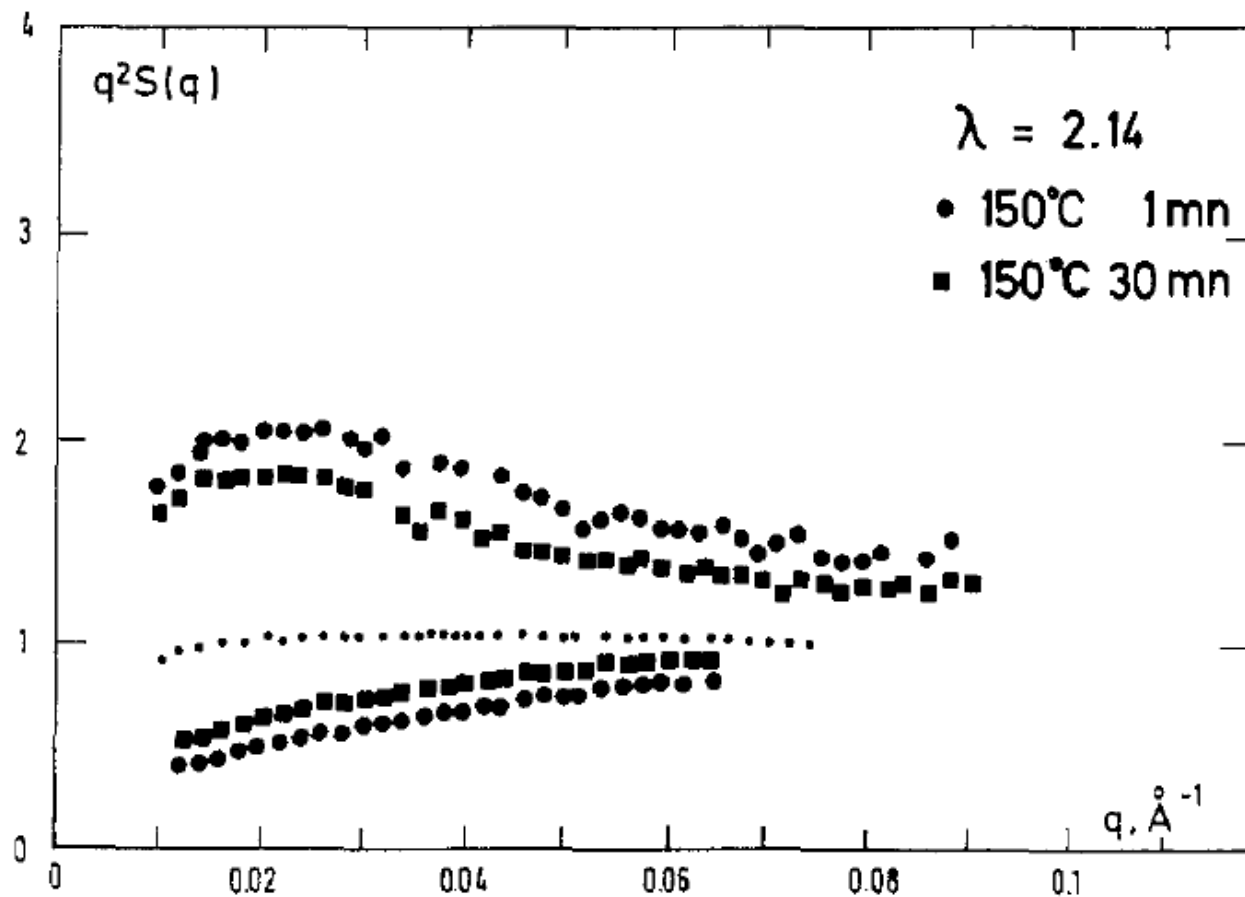
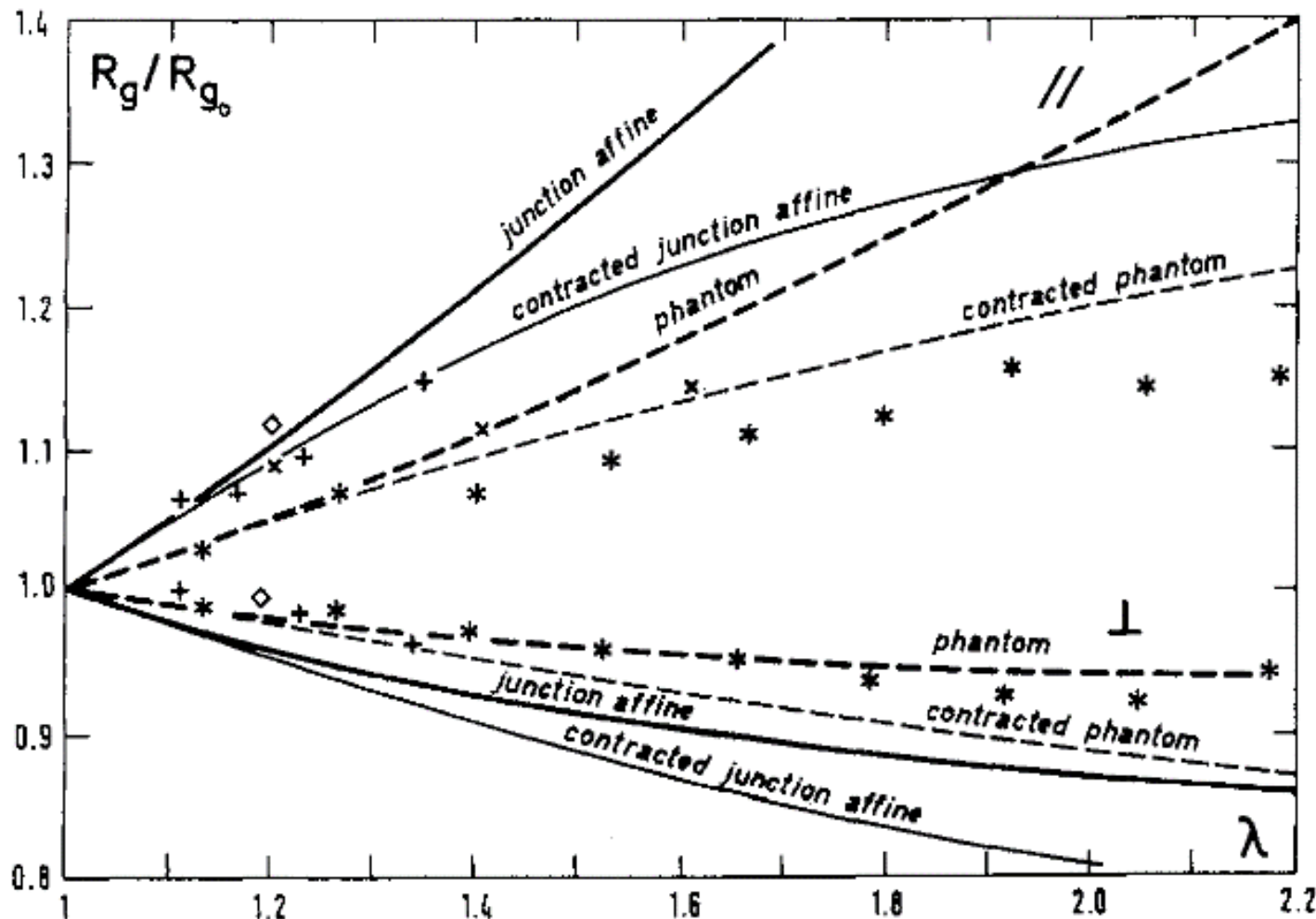


Fig. 5. Relaxation of the form factor of a γ -rubber stretched 2.14 times between 1 min (●) and 30 min (■) at 150°C

Labelled meshes, in

Progr Colloid & Polymer Sci
75:152-170 (1987)

Studies of network deformation: mechanical models



Phantom network vs. junction-affine
Happy? Good fit? Different deformations in
two directions! => Defects

Labelled meshes, in
Progr Colloid & Polymer Sci
75:152-170 (1987)

Outline

Examples

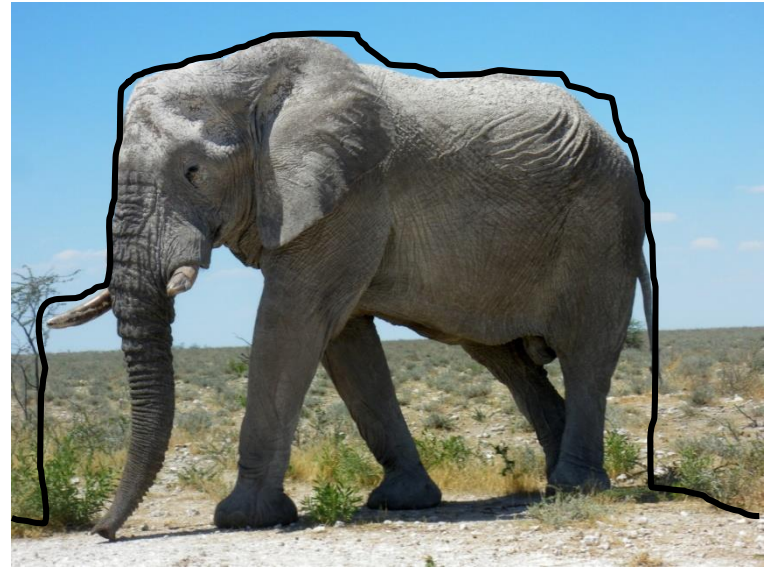
- Chains in polymer nanocomposites.
- Chains in core-shell microgel particles.

Chains can be modelled as sequence of beads/monomers.

- NPs in polymer nanocomposites: simple RMC
- Aggregates of NPs in polymer nanocomposites: RMC+aggs
- Anisotropy: field- or deformation-induced.

Take home messages

- It is said to take five parameters to fit an elephant.
- A good fit does NOT mean you have produced anything meaningful.



THEREFORE (true for many areas):

- Start with **easiest model**. Only in case of failure, make it more complex (more parameters, phenomena, ...).
- Don't try to make perfect fits. Better follow **signatures** (slopes, peaks, ...).
- **Talk to people** with experience in data treatments.
- Use other people's programs only if you **understand** what you are doing (namely, the underlying equations).

What (neutron) scattering really is...

